

Queue ADT

Tiziana Ligorio

Today's Plan



Announcements

Queue ADT

Applications

Queue

A data structure representing a waiting line

Objects can be **enqueued** to the back of the line

or **dequeued** from the front of the line



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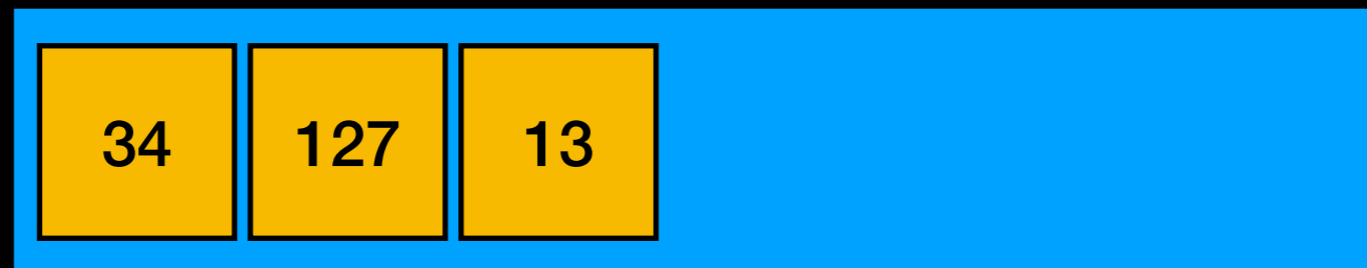


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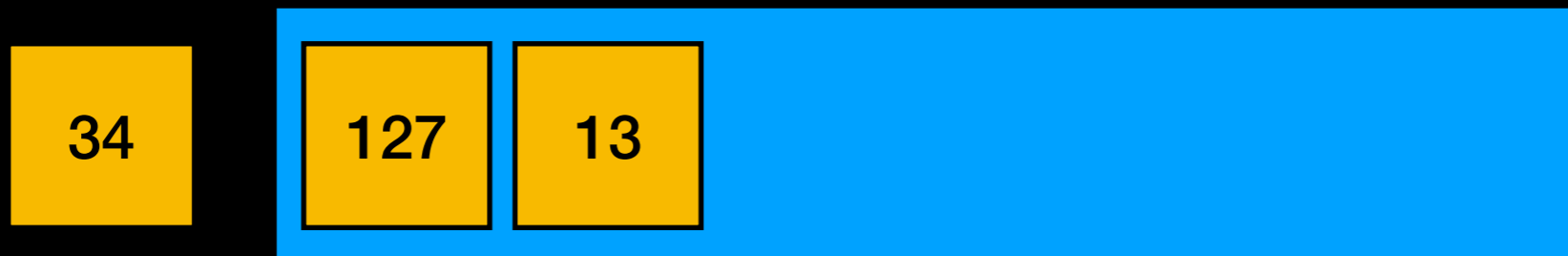


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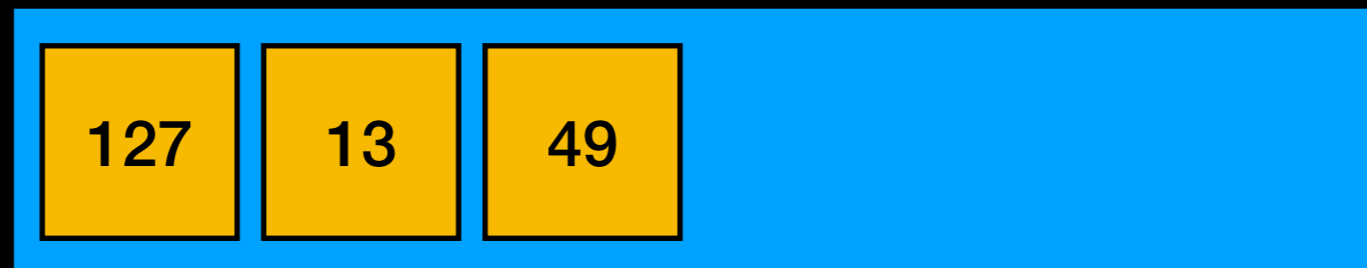


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FIFO: First In First Out

Only front of queue is accessible (**front**), no other objects in the queue are visible

Queue Applications

Generating all substrings

Recognizing Palindromes

Any waiting queue

- Print jobs
- OS scheduling processes with equal priority
- Messages between asynchronous processes

...

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Generating all substrings

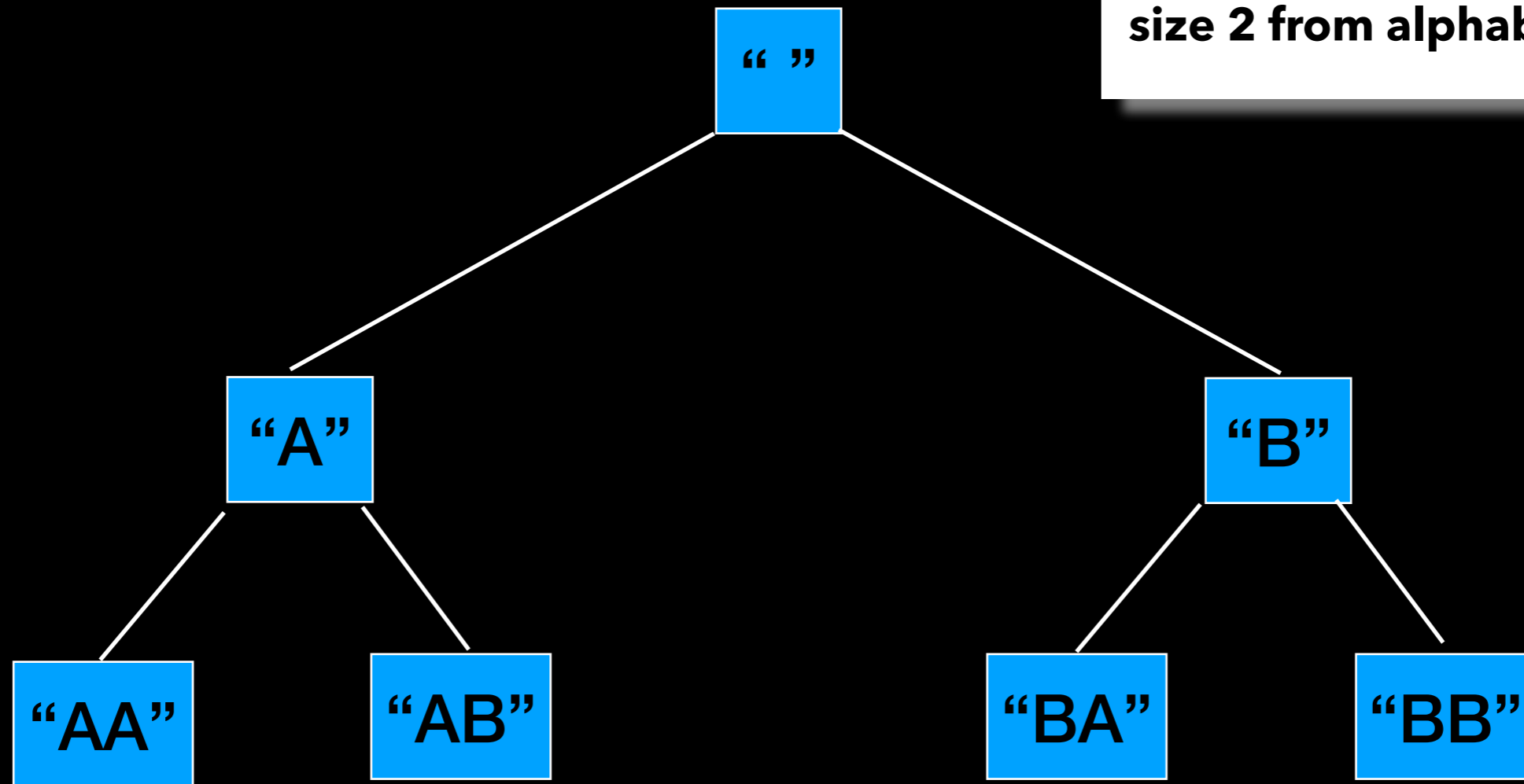
Generate all possible strings **up to** some fixed length **n** **with repetition (same character included multiple times)**

We saw how to do something similar recursively (generate permutations of **fixed size n no repetition**)

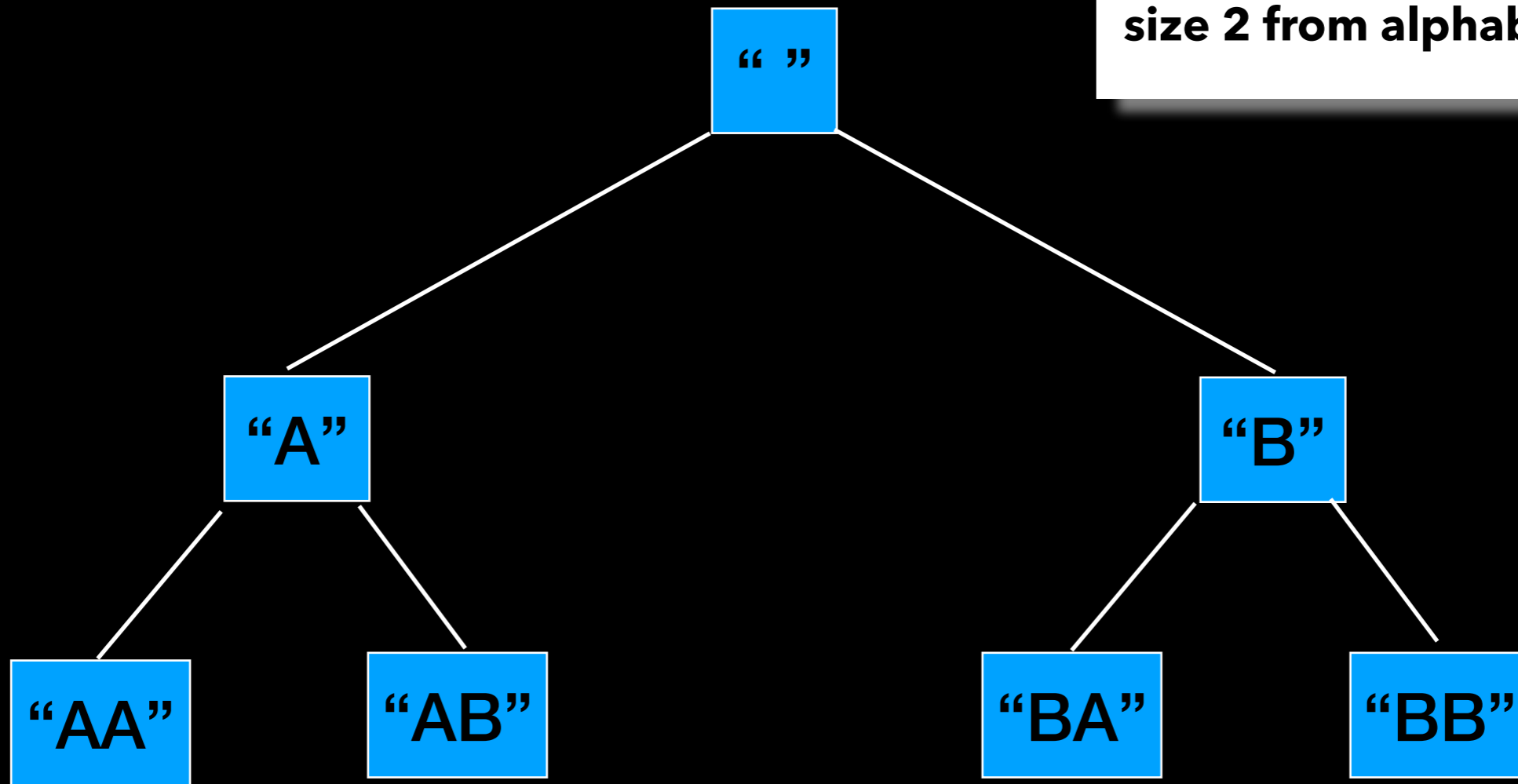
How might we do it with a queue?

Example simplified to $n = 2$ and only letters A and B

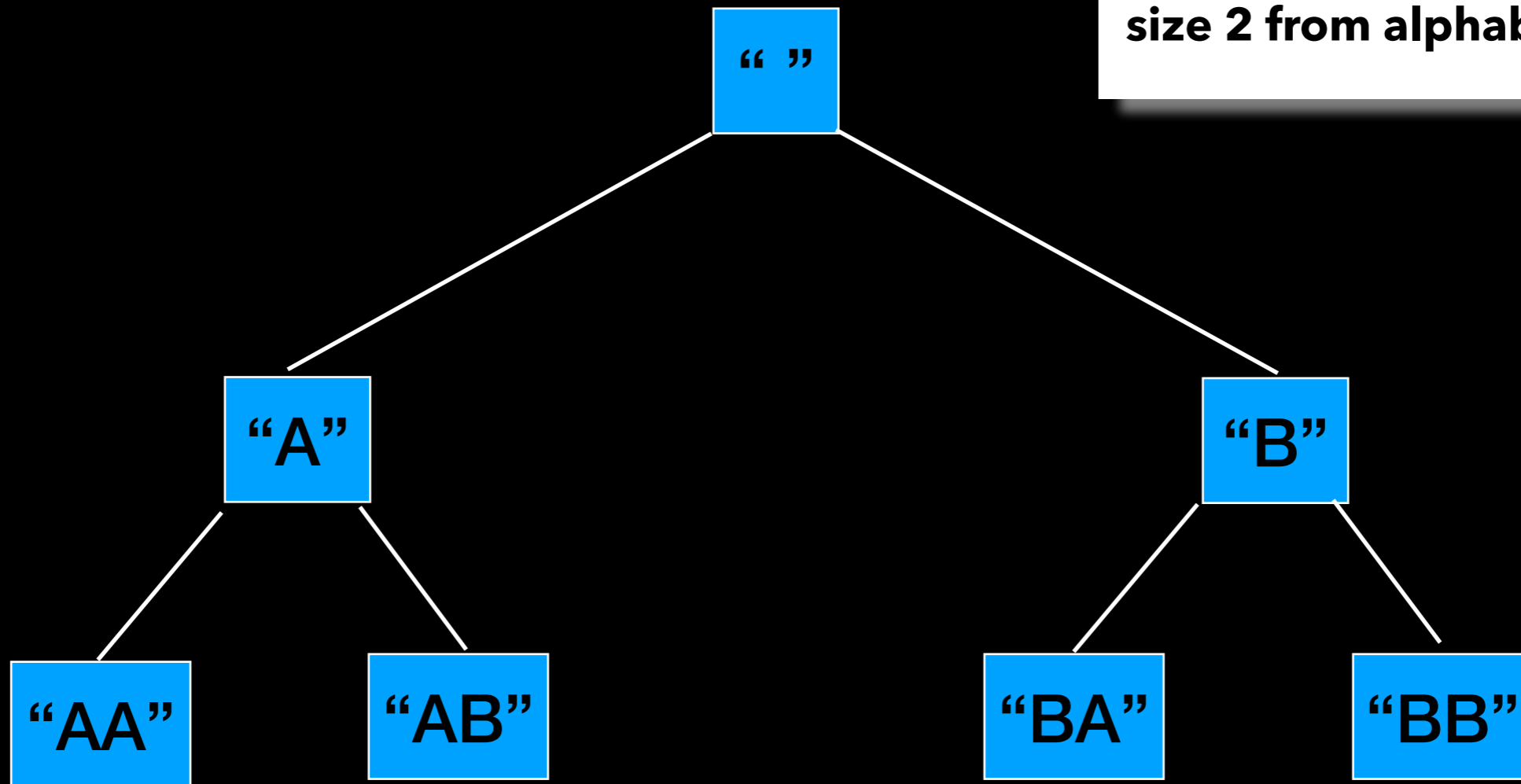
Generate all substrings of size 2 from alphabet {'A', 'B'}



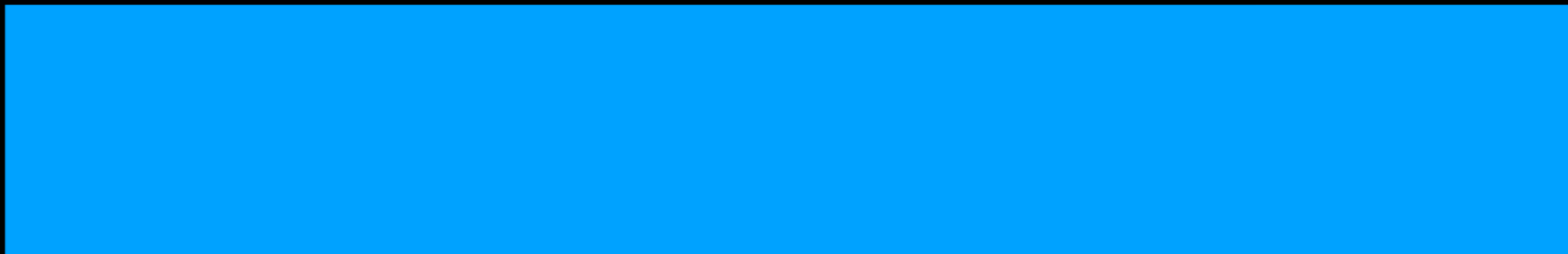
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Generate all substrings of size 2 from alphabet {'A', 'B'}

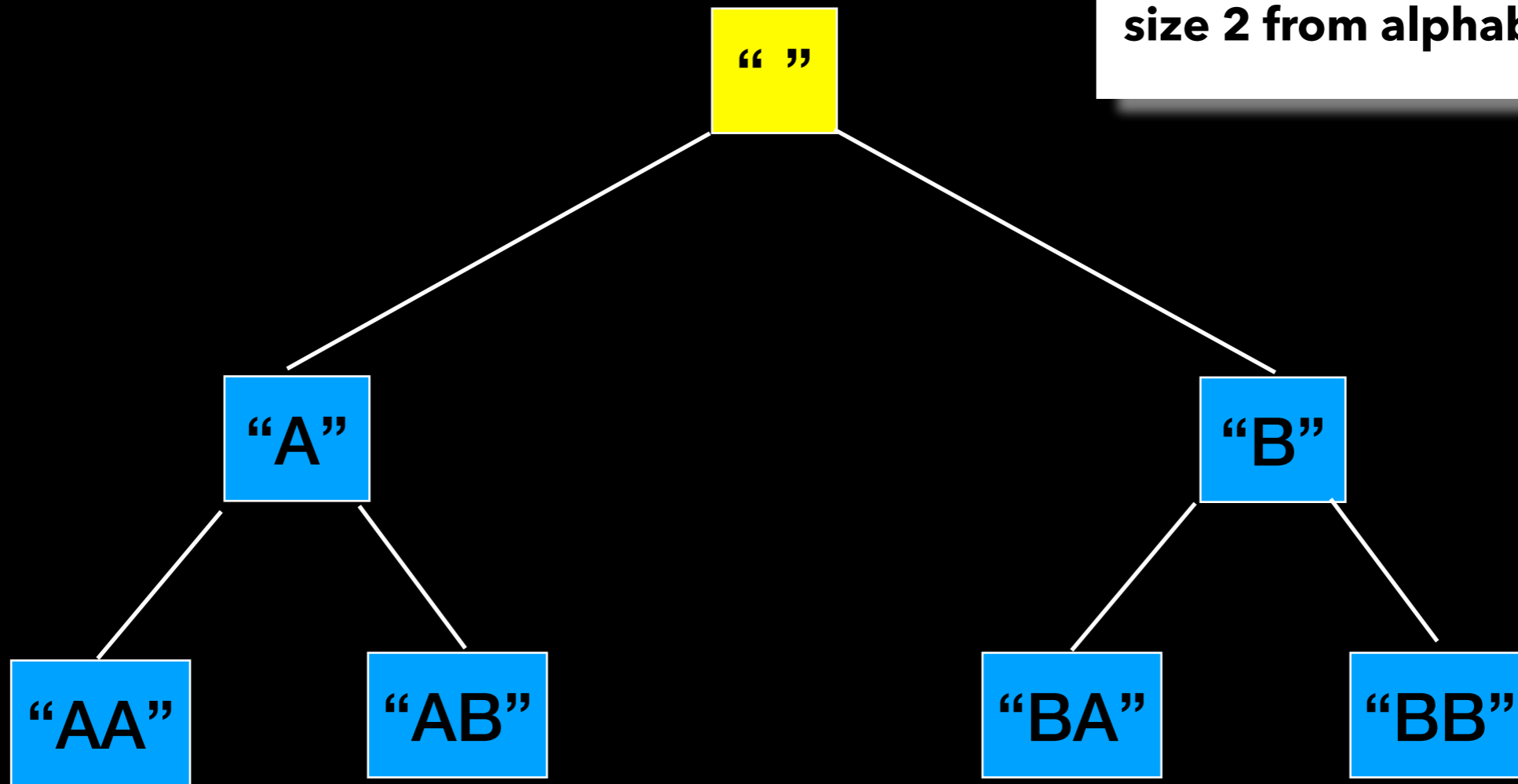


“ ”



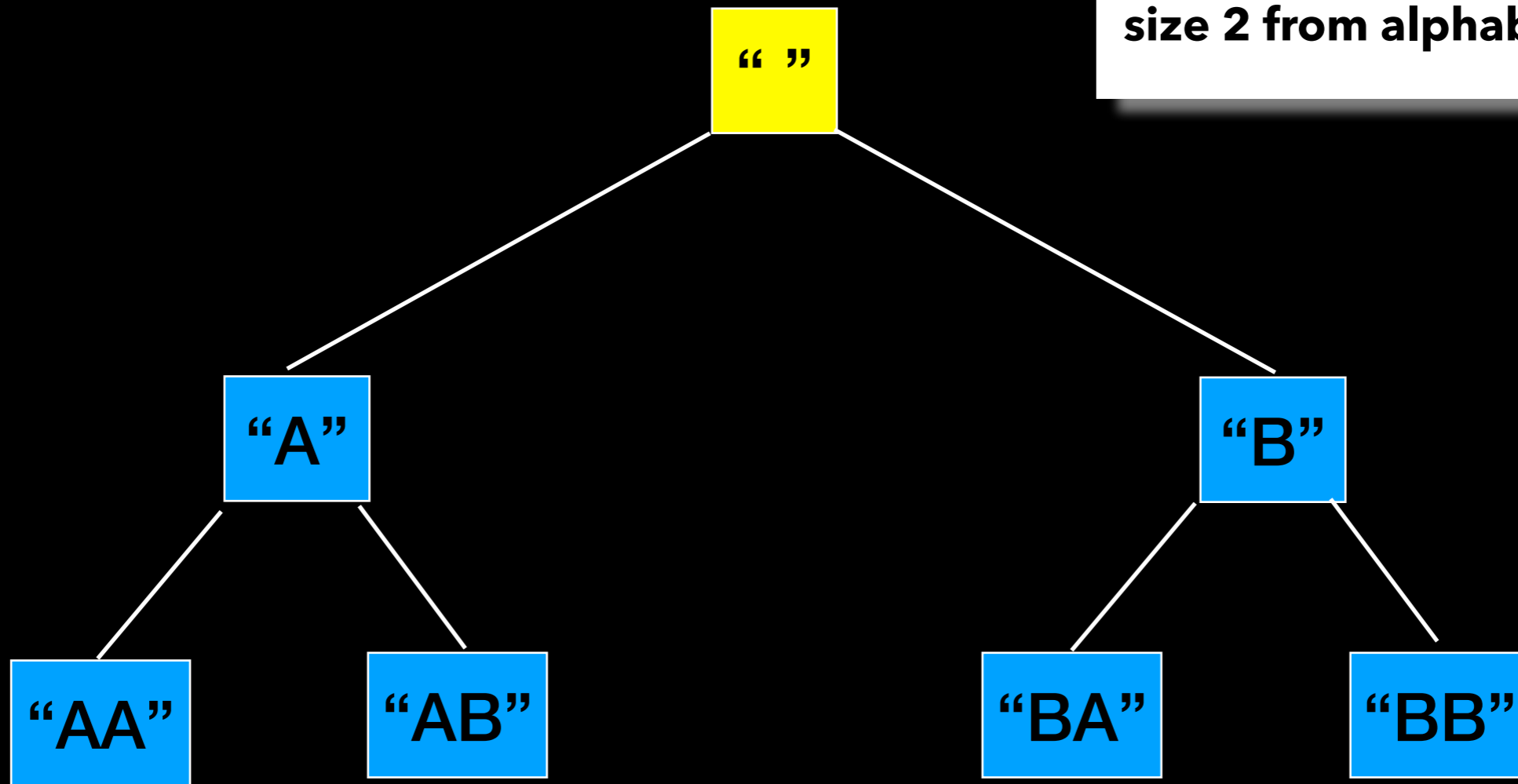
{ "" }

Generate all substrings of size 2 from alphabet {'A', 'B'}



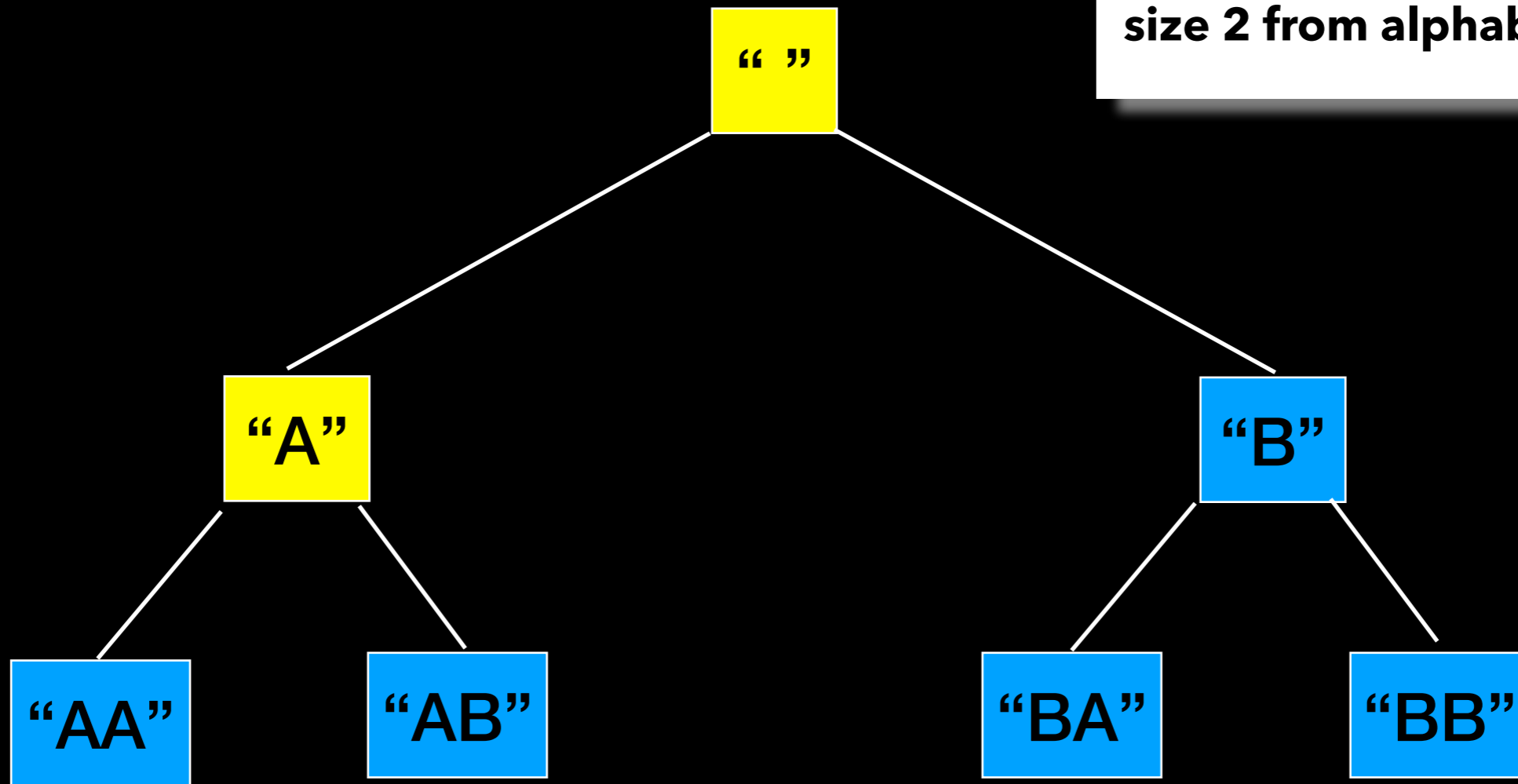
{ "" }

Generate all substrings of size 2 from alphabet {'A', 'B'}



{ "", "A" }

Generate all substrings of size 2 from alphabet {'A', 'B'}

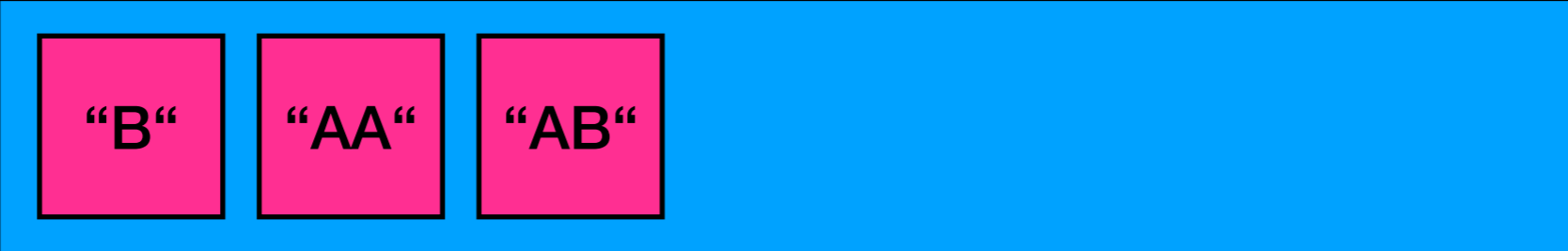
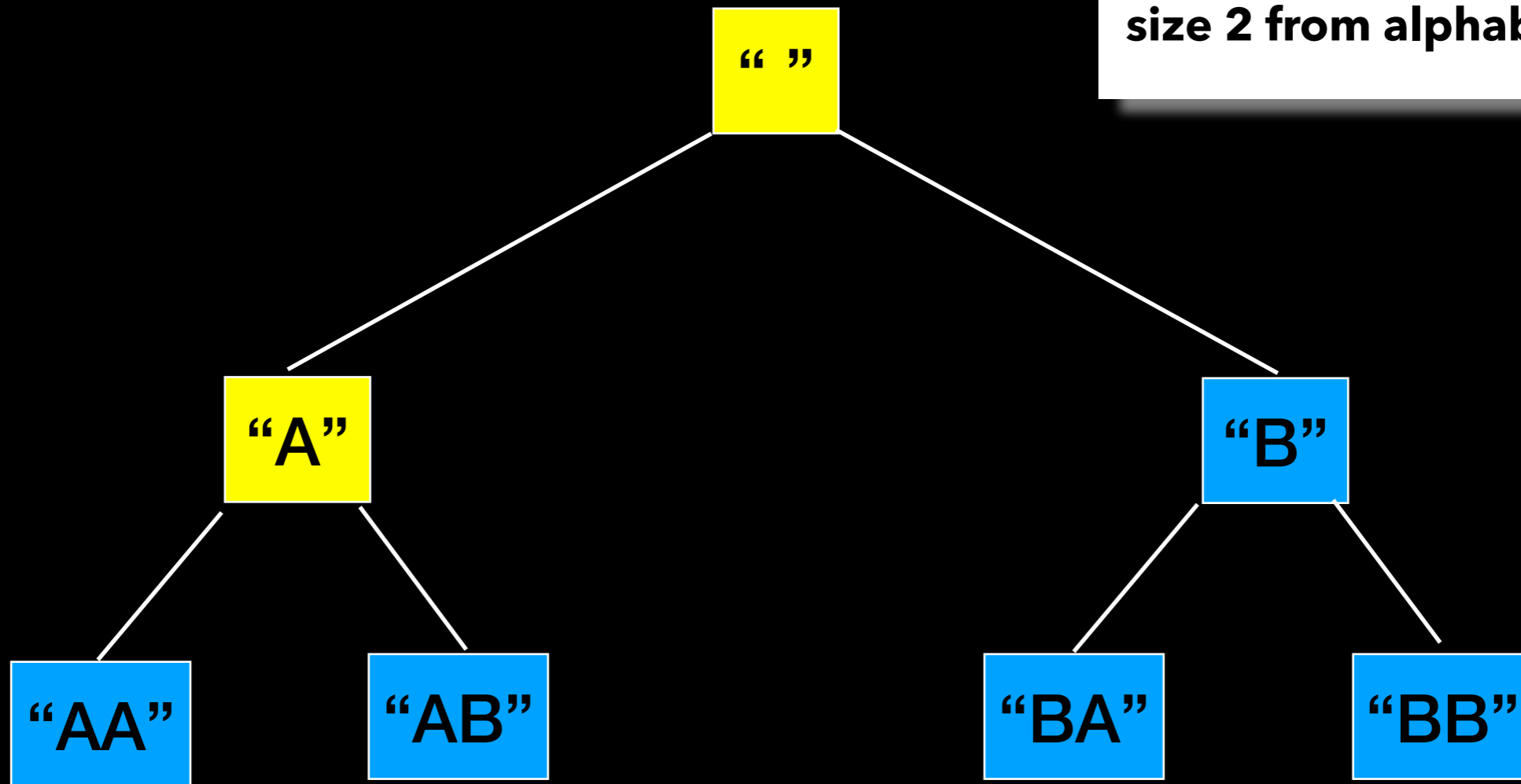


“A“ “AA“ “AB“

“B“

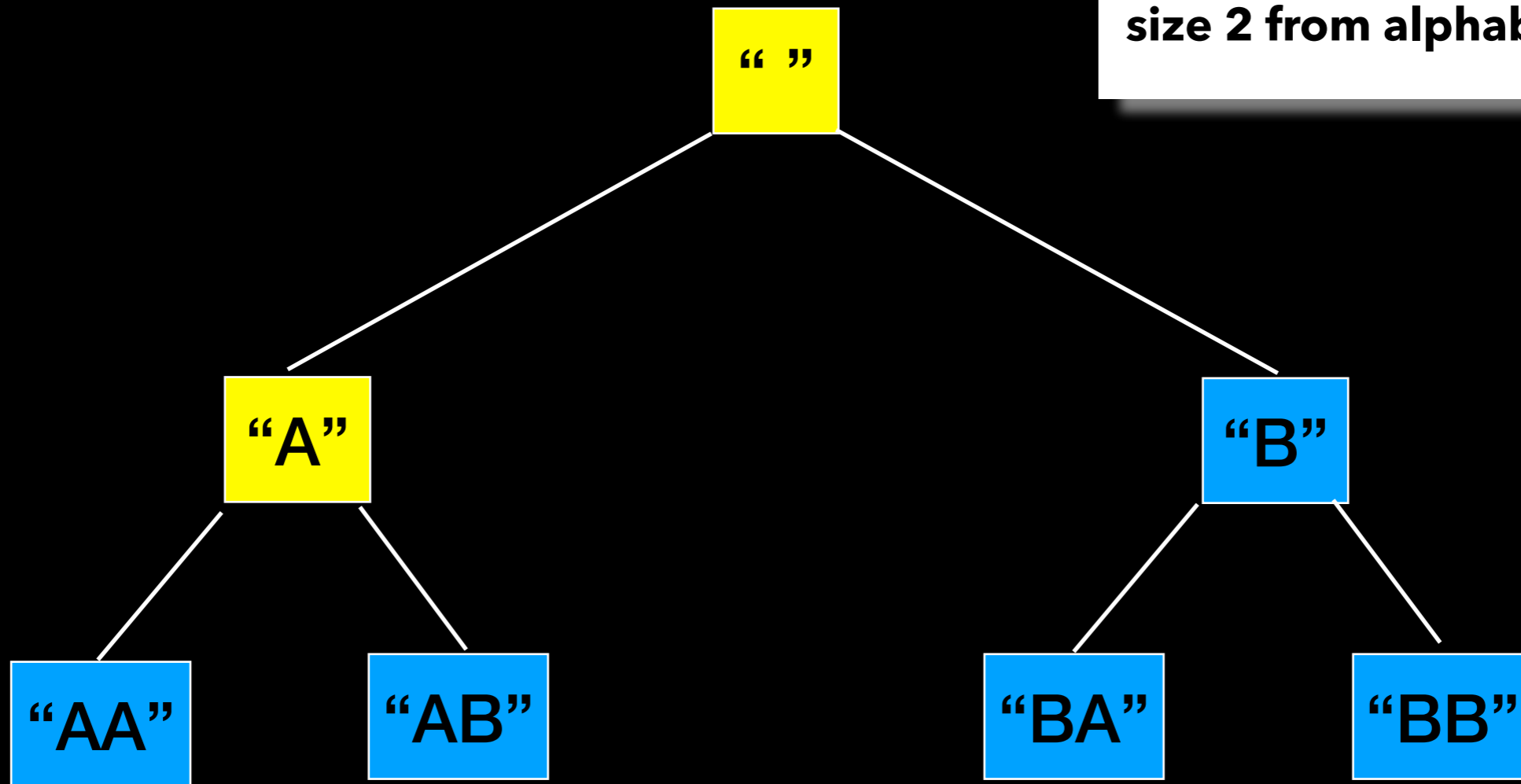
{ "", "A" }

Generate all substrings of size 2 from alphabet {'A', 'B'}



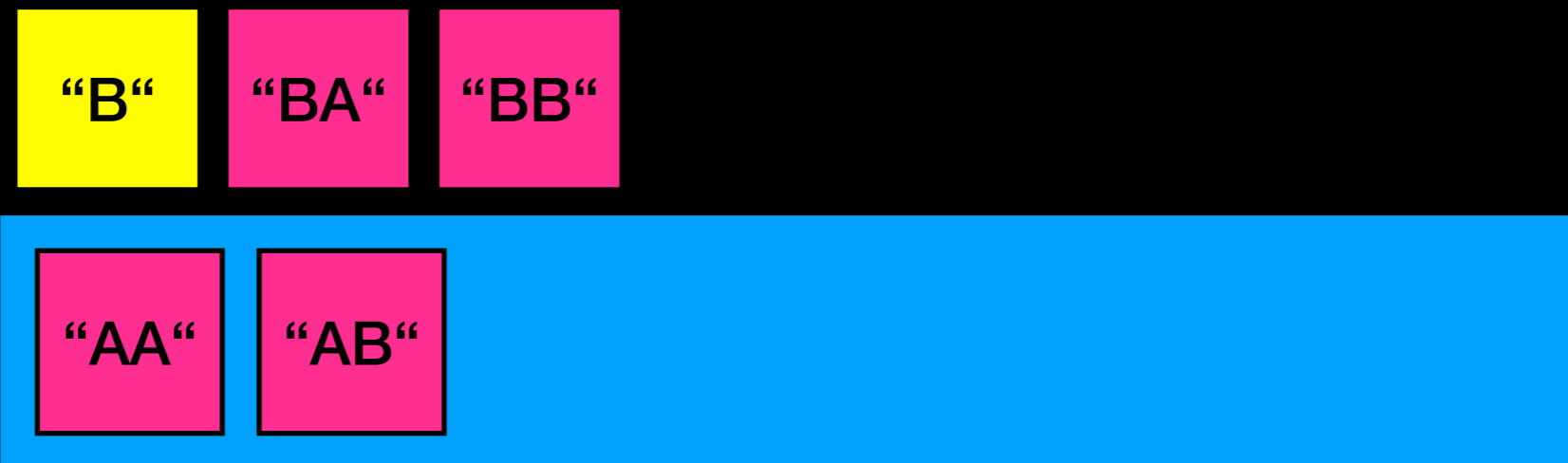
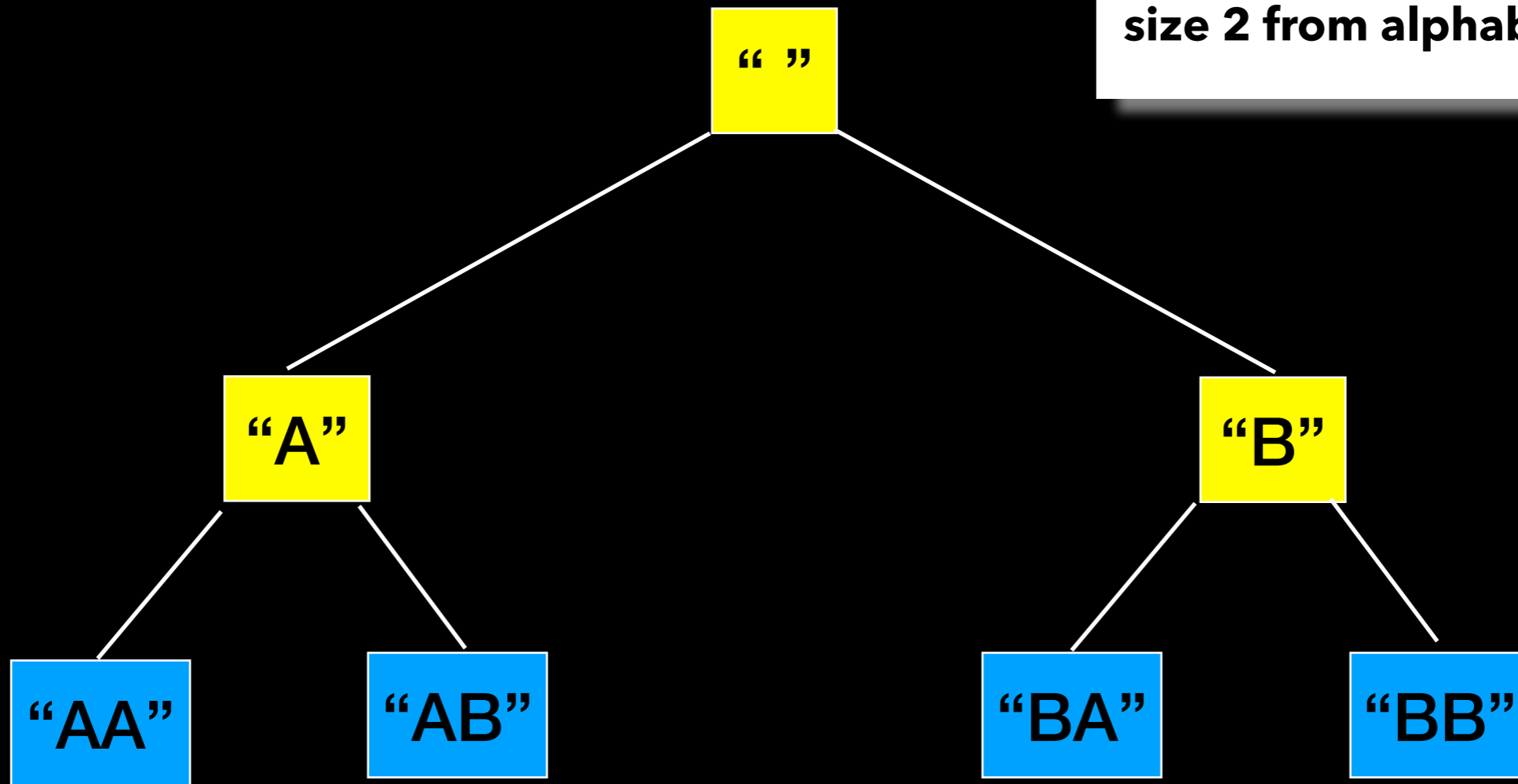
{ "", "A" }

Generate all substrings of size 2 from alphabet {'A', 'B'}



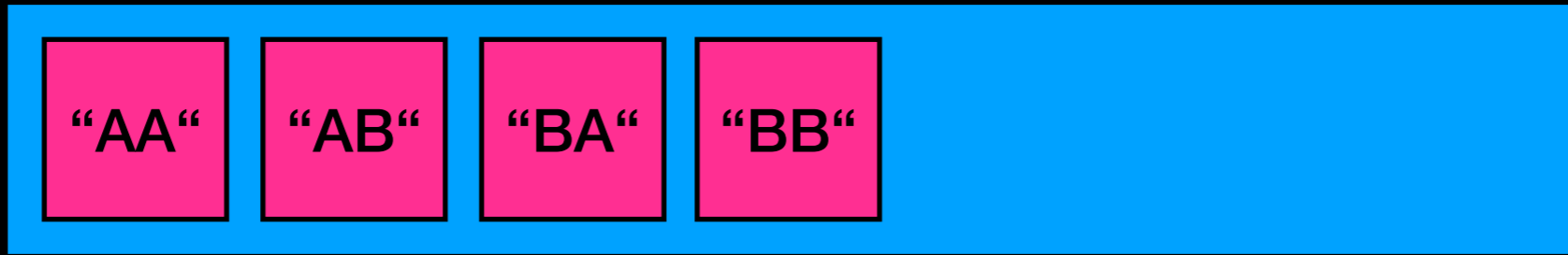
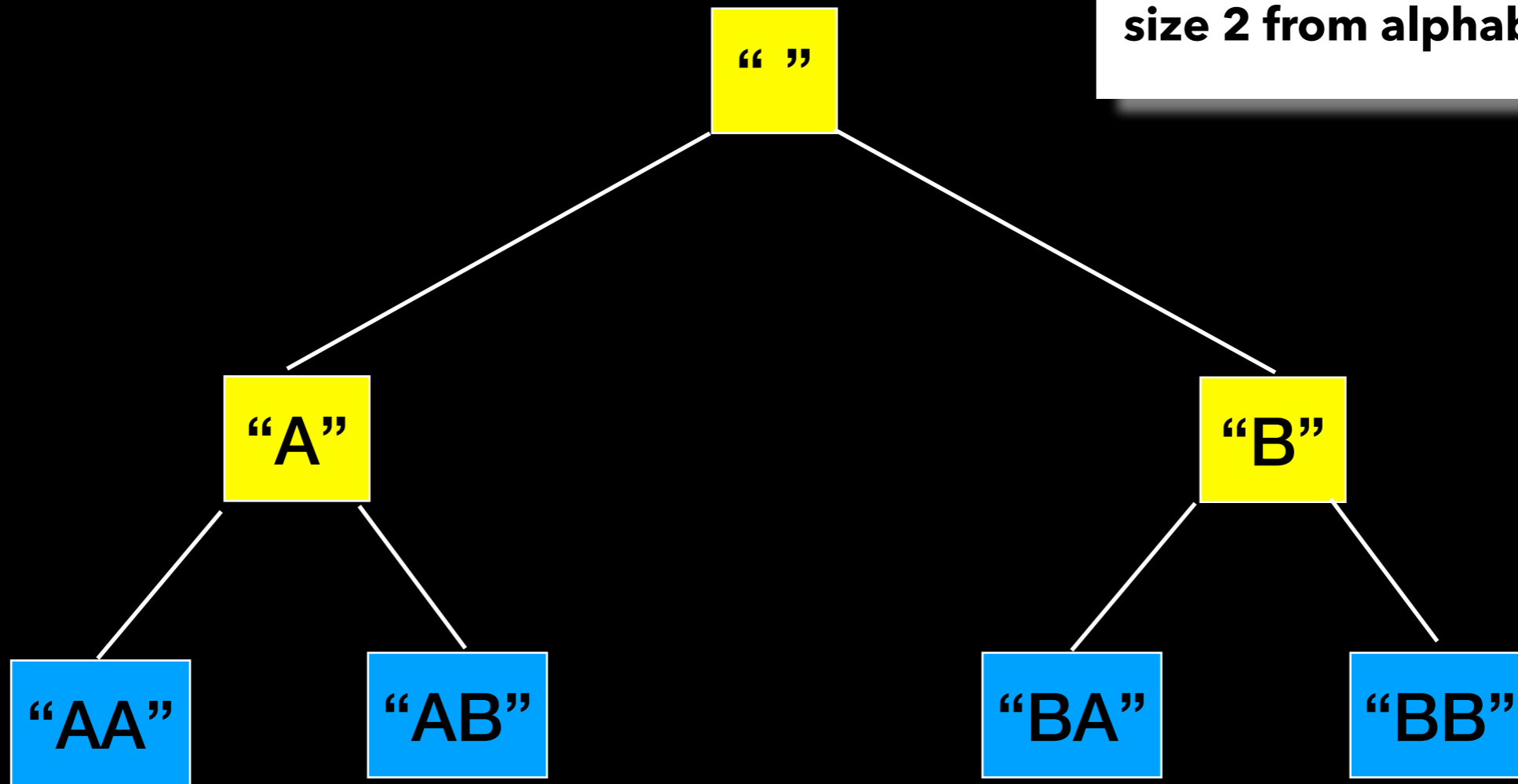
{ "", "A", "B" }

Generate all substrings of size 2 from alphabet {'A', 'B'}



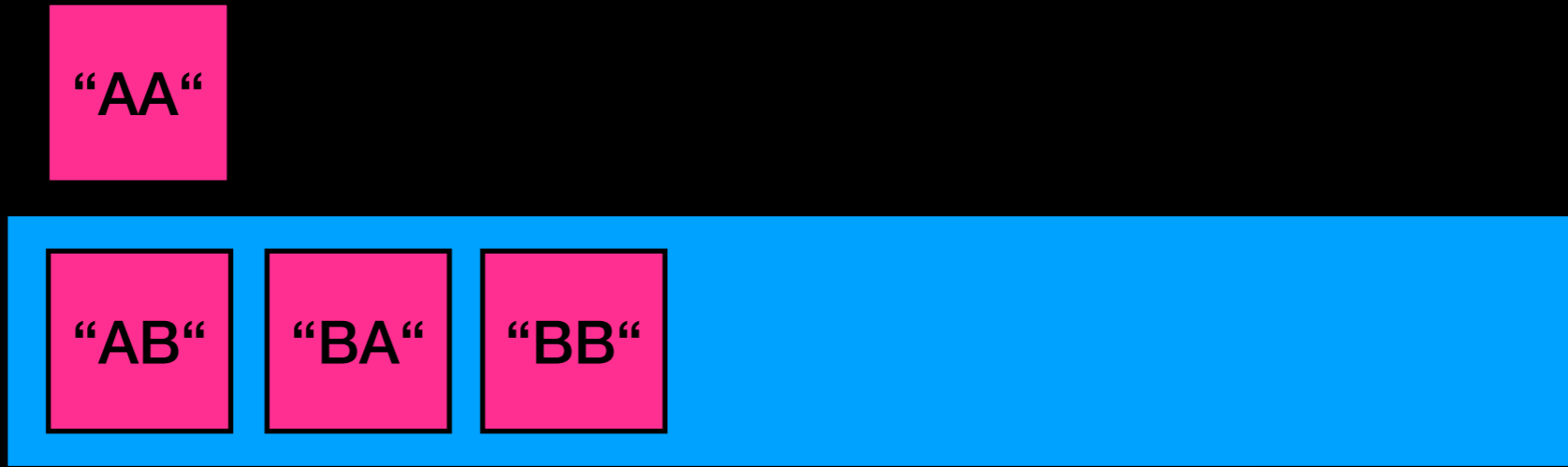
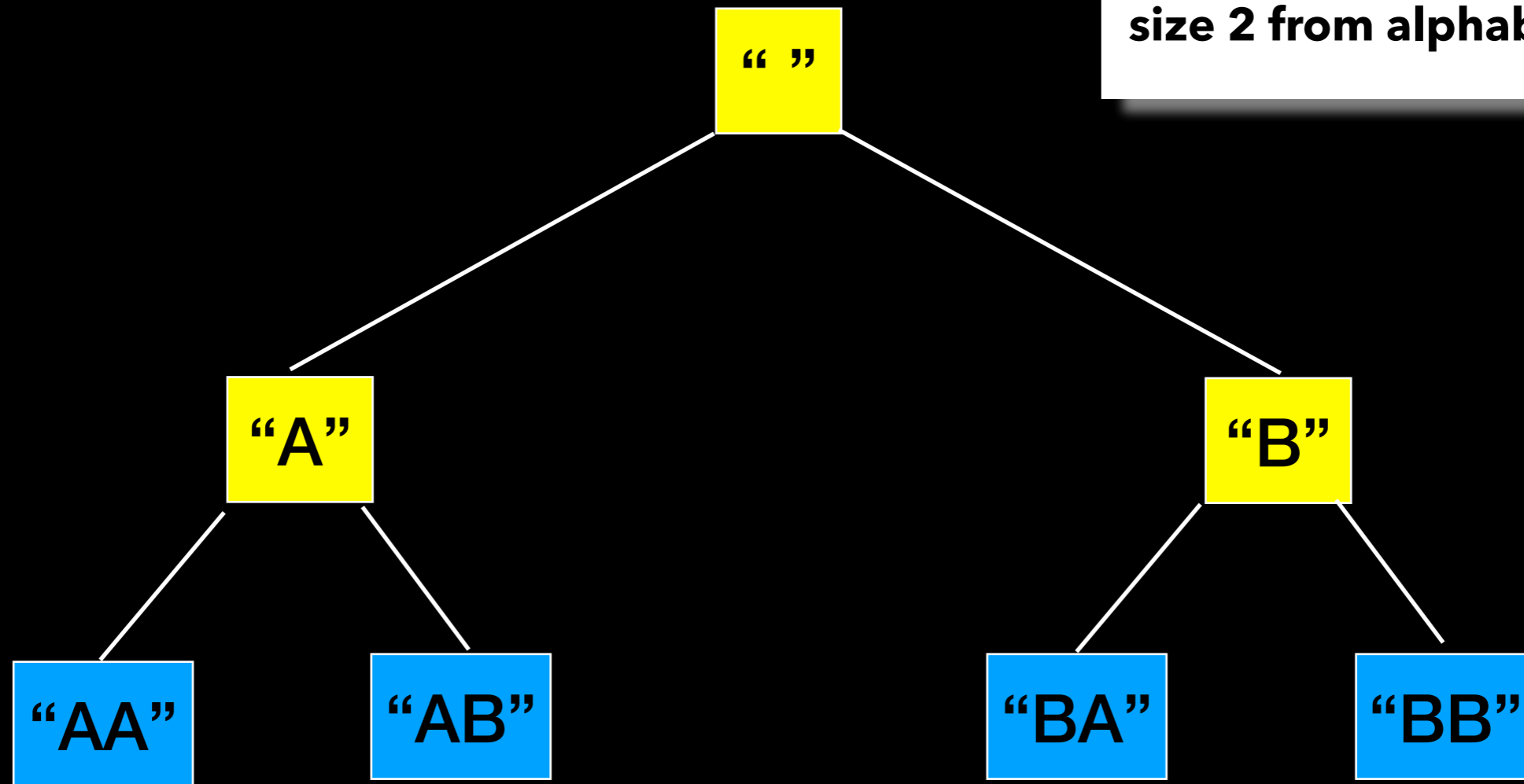
{ "", "A", "B" }

Generate all substrings of size 2 from alphabet {'A', 'B'}



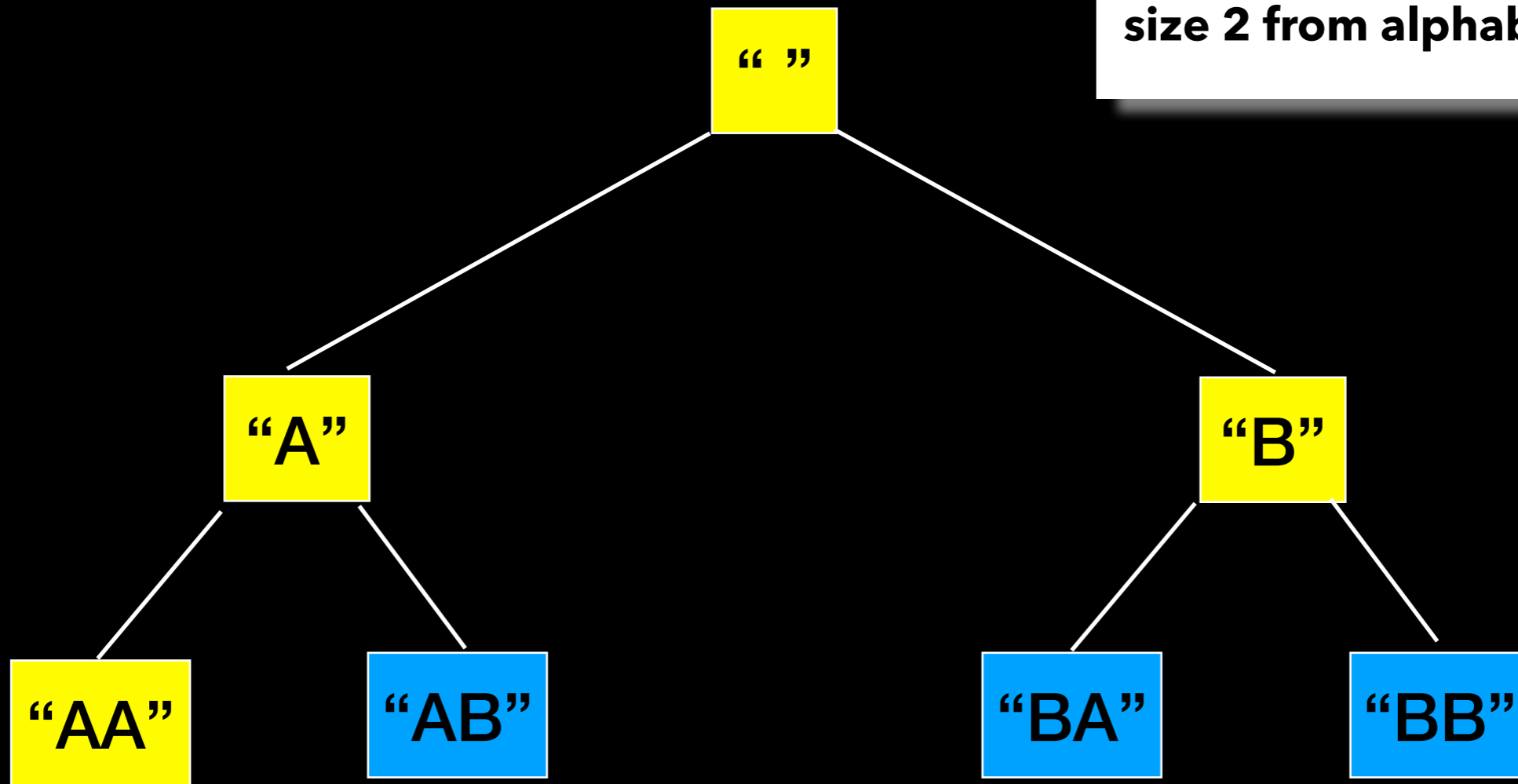
{ "", "A", "B" }

Generate all substrings of size 2 from alphabet {'A', 'B'}

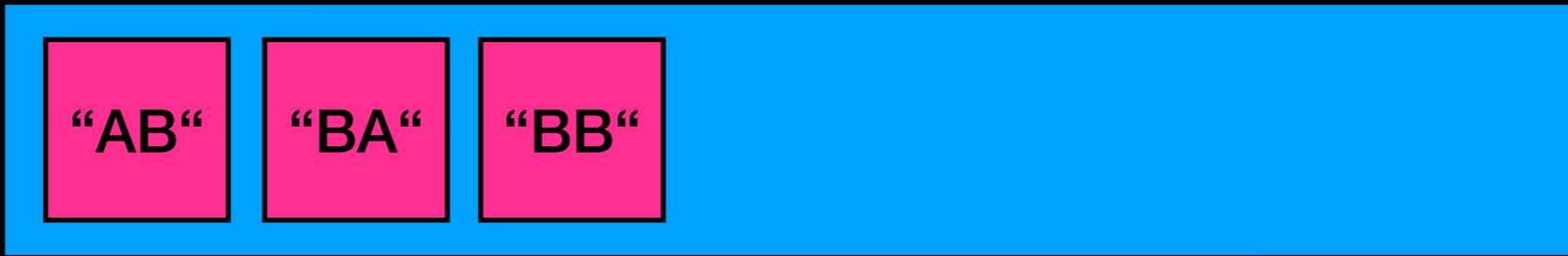


{ "", "A", "B", "AA" }

Generate all substrings of size 2 from alphabet {'A', 'B'}

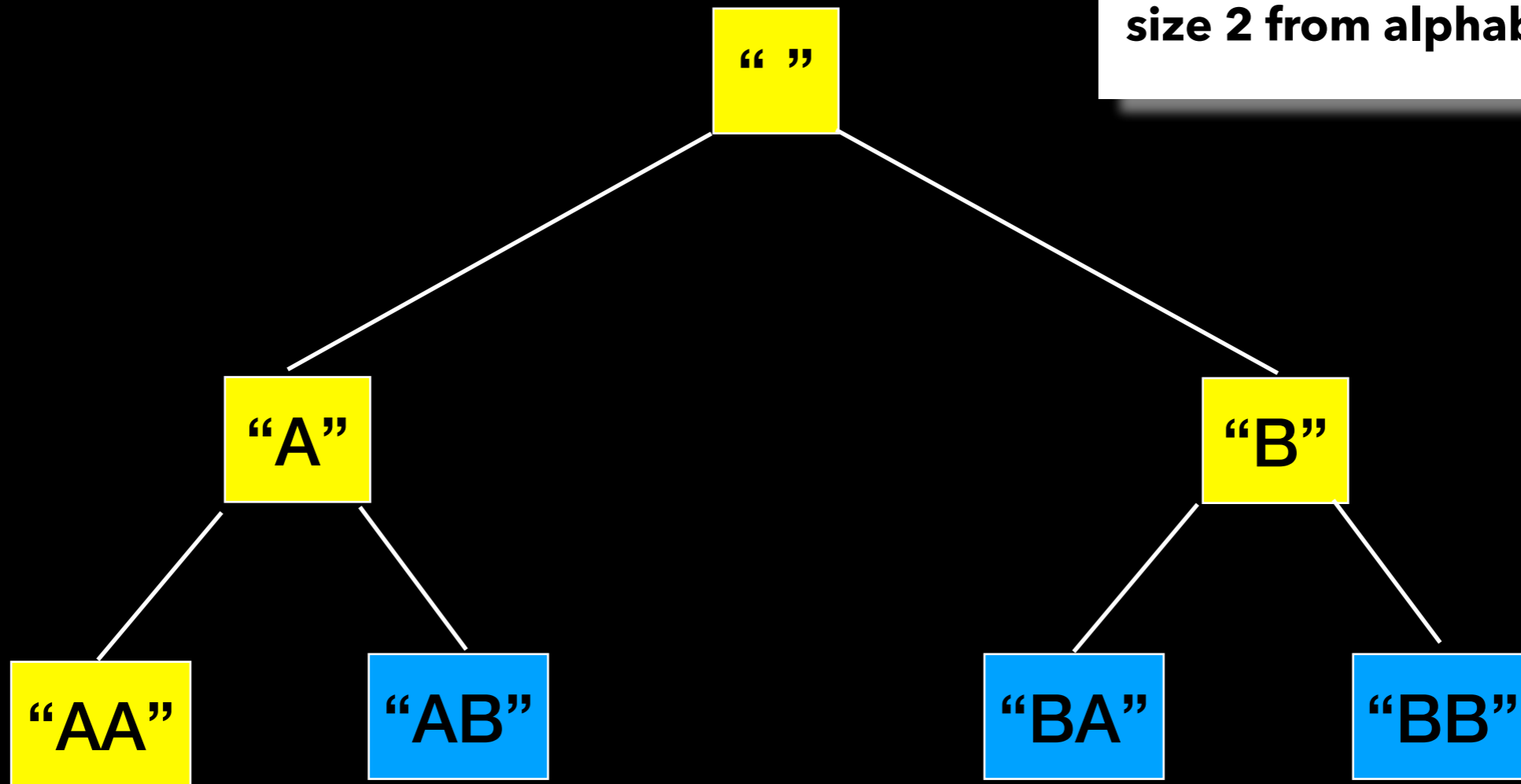


“AA“



{ "", "A", "B", "AA" }

Generate all substrings of size 2 from alphabet {'A', 'B'}

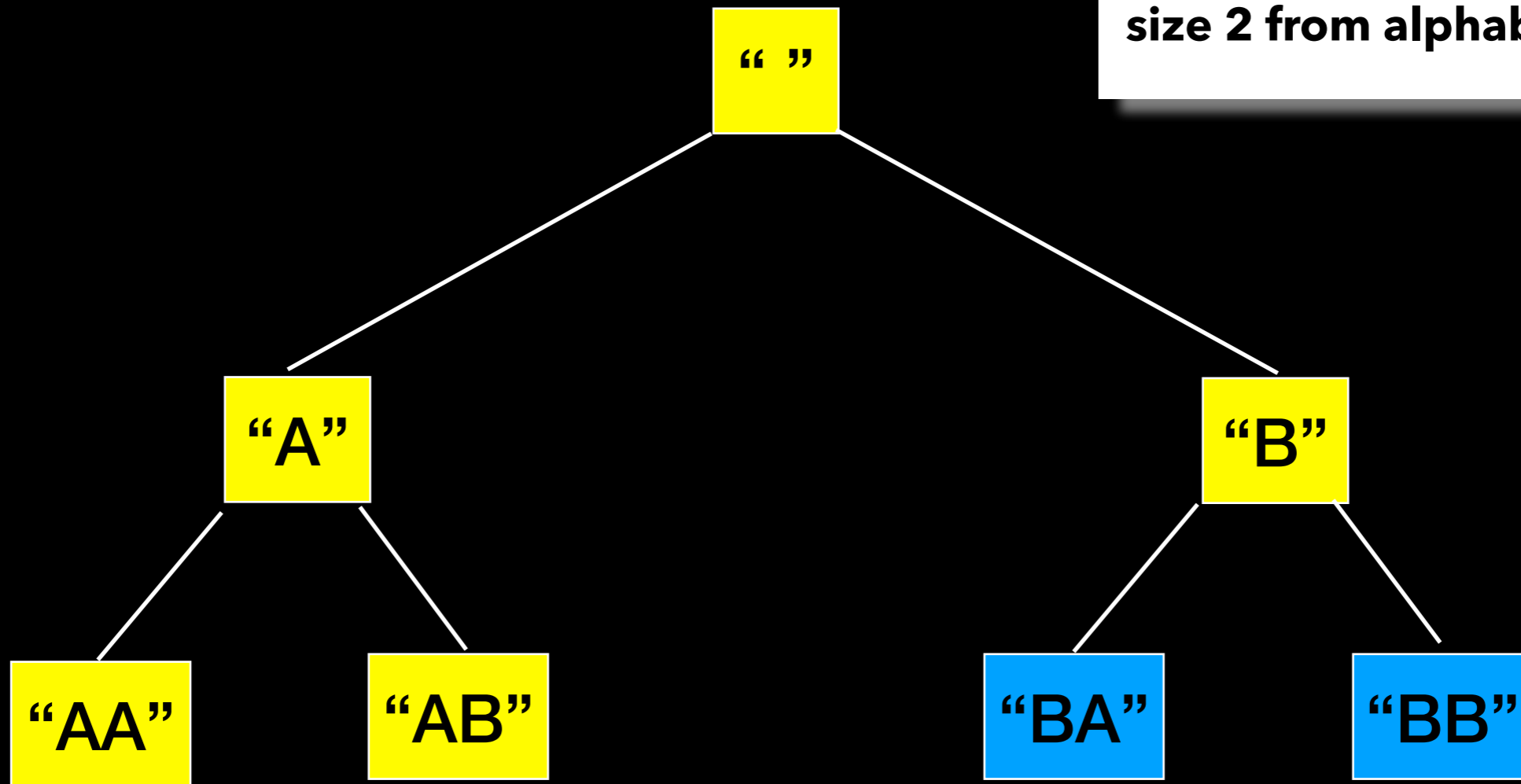


“AB“

“BA“ “BB“

{ "", "A", "B", "AA", "AB" }

Generate all substrings of size 2 from alphabet {'A', 'B'}

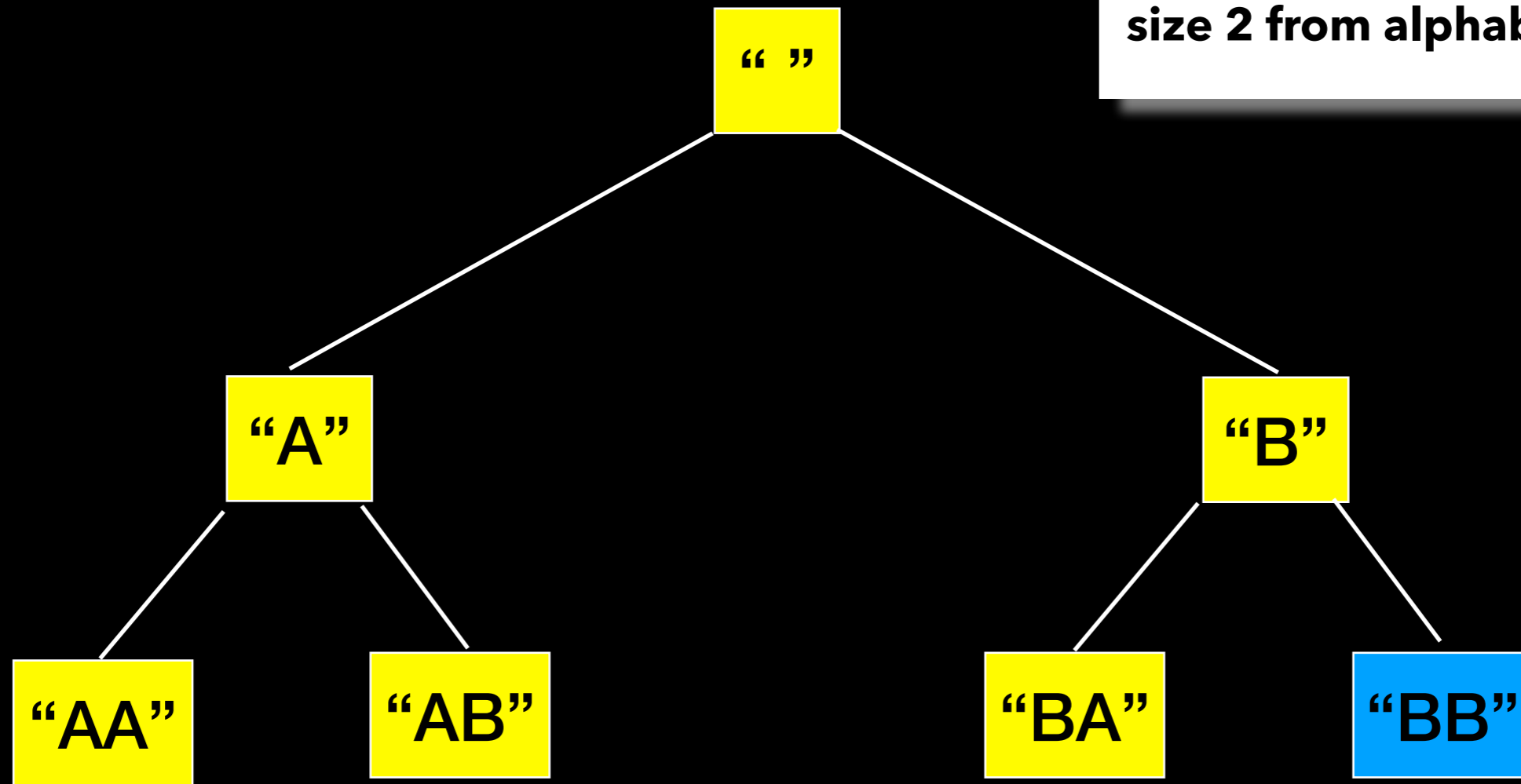


"AB"



{ "", "A", "B", "AA", "AB", "BA" }

Generate all substrings of size 2 from alphabet {'A', 'B'}

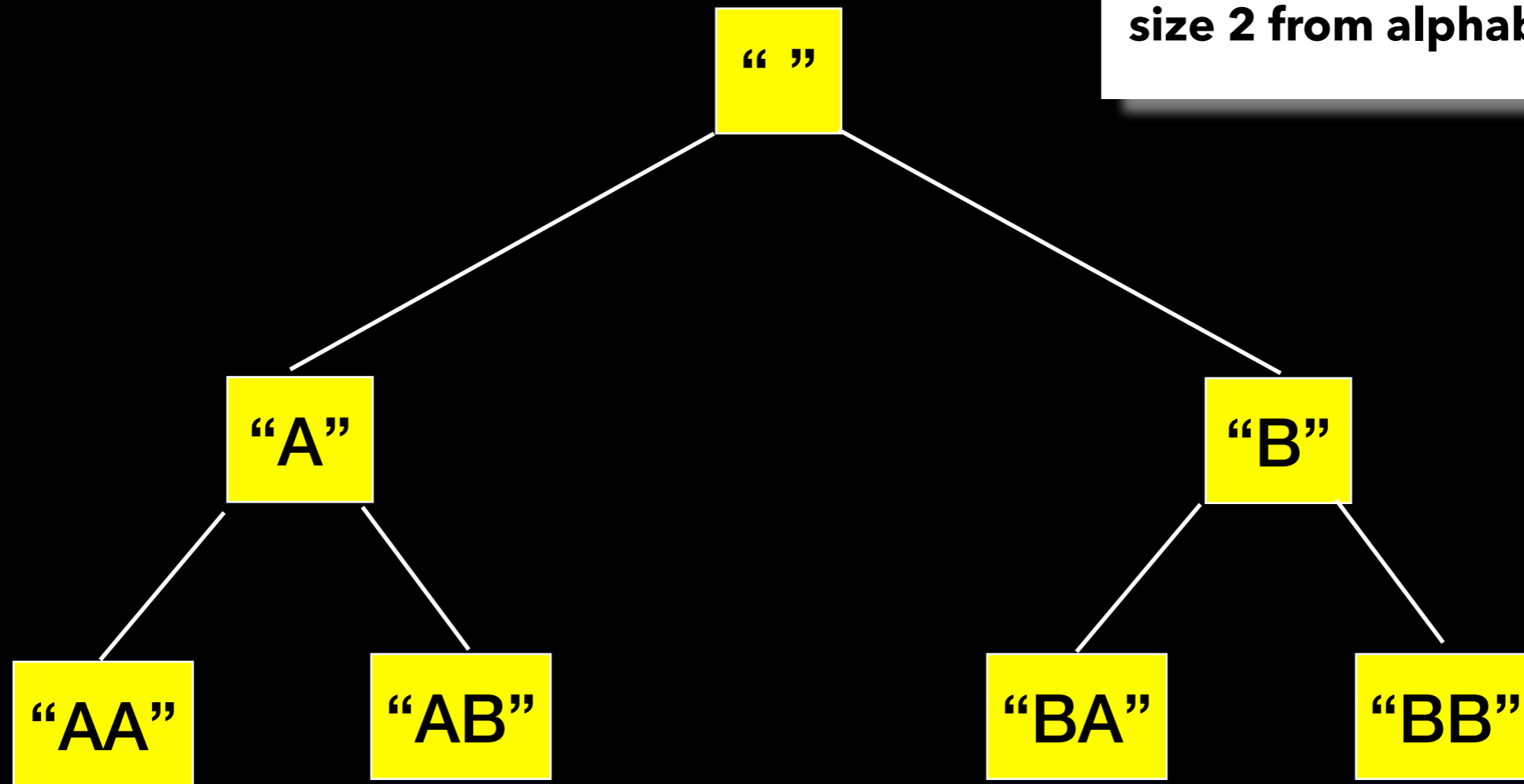


“BA“

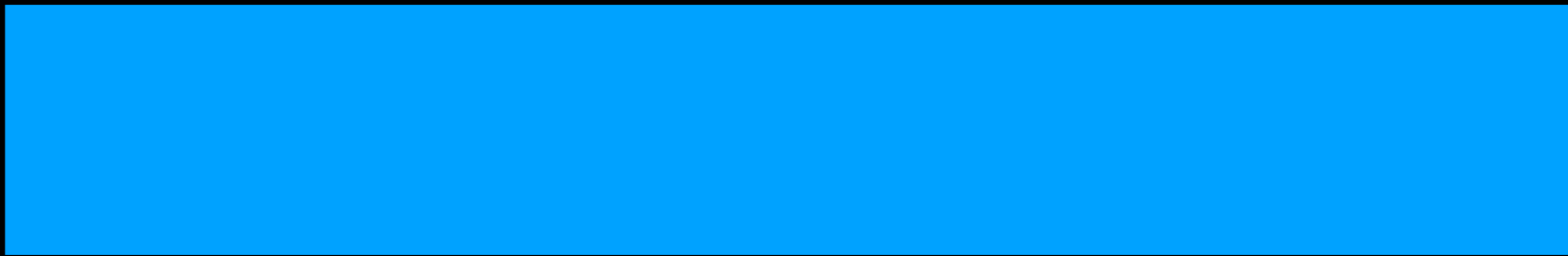
“BB“

{ "", "A", "B", "AA", "AB", "BA", "BB" }

Generate all substrings of size 2 from alphabet {'A', 'B'}

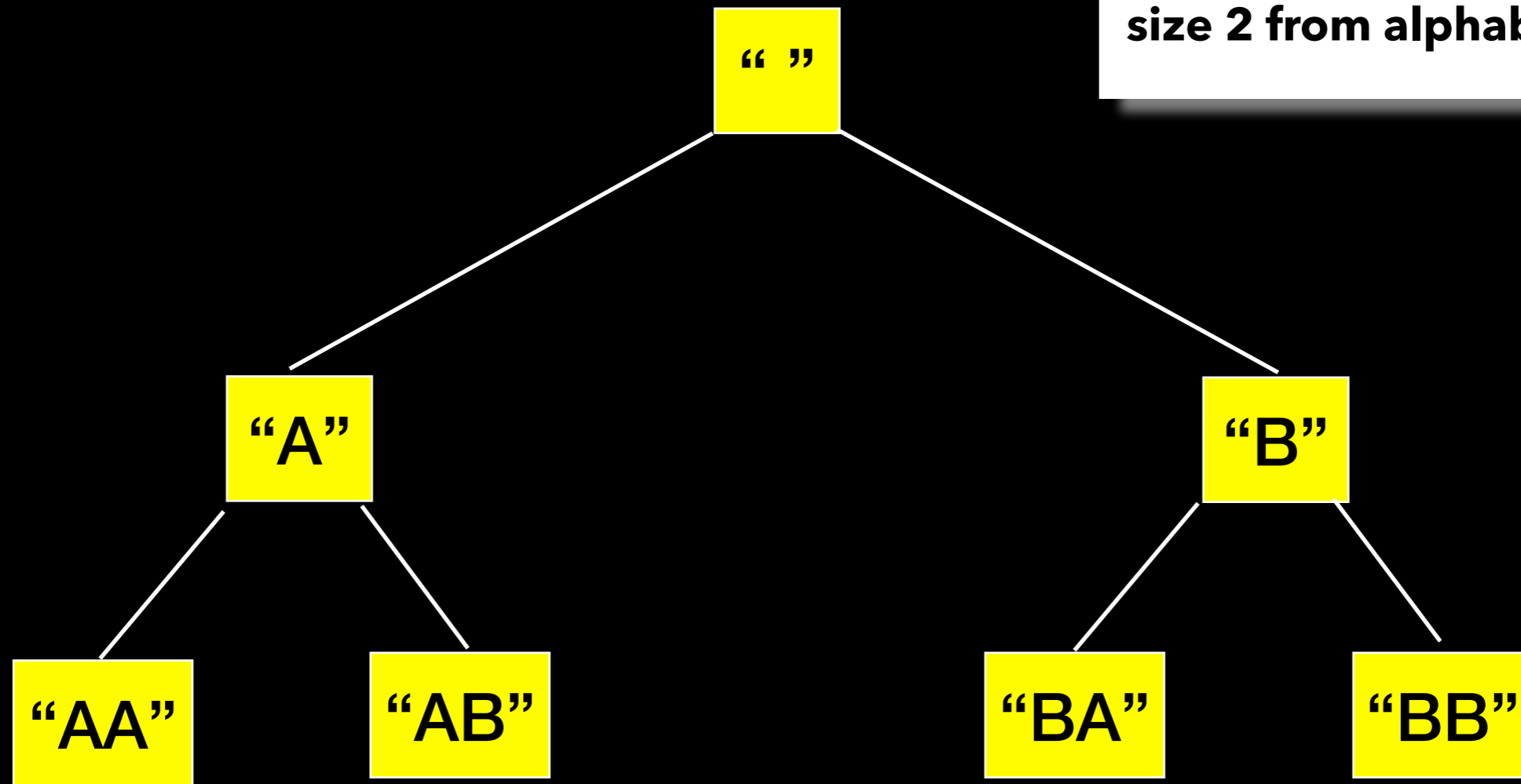


“BB“



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Generate all substrings of size 2 from alphabet {'A', 'B'}



Breadth-First Search

Applications

Find shortest path in graph

GPS navigation systems

Crawlers in search engines

...

Generally good when looking for the "shortest" or "best" way to do something => lists things in increasing order of "size" stopping at the "shortest" solution

Size of Substring

```
findAllSubstrings(int n)
{
    put empty string on the queue


    while(queue is not empty){
        let current_string = dequeue and add to result
        if(size of current_string < n){
            for(each character ch)//every character in alphabet
                append ch to current_string and enqueue it
        }
    }
    return result;
}
```

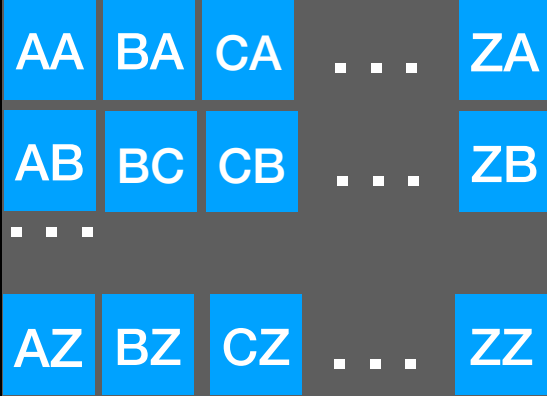
Analysis

Finding all substrings (with repetition) of size **up to n**

Assume **alphabet** (A, B, ..., Z) of size 26

The empty string = $1 = 26^0$ 

All strings of size 1 = 26^1 

All strings of size 2 = 26^2 

...

All strings of size n = 26^n

With repetition: I have 26 options for each of the n characters

Lecture Activity

Size of Substring

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Analyze the worst-case time complexity of this algorithm assuming alphabet of size 26 and up to strings of length n

$T(n) = ?$

$O(?)$

Will stop when all strings have been removed from queue

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Will stop when all strings have been removed from queue

Removes 1 string from the queue

Adds 26 strings to the queue

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        }
    }
    return result;
}
```

Loop until queue is empty and dequeue only 1 each time.

So the question becomes:

How many strings are enqueued in total?

Will stop when all strings have been removed from queue

Removes 1 string from the queue

Adds 26 strings to the queue

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$$T(n) = 26^0 + 26^1 + 26^2 + \dots + 26^n$$

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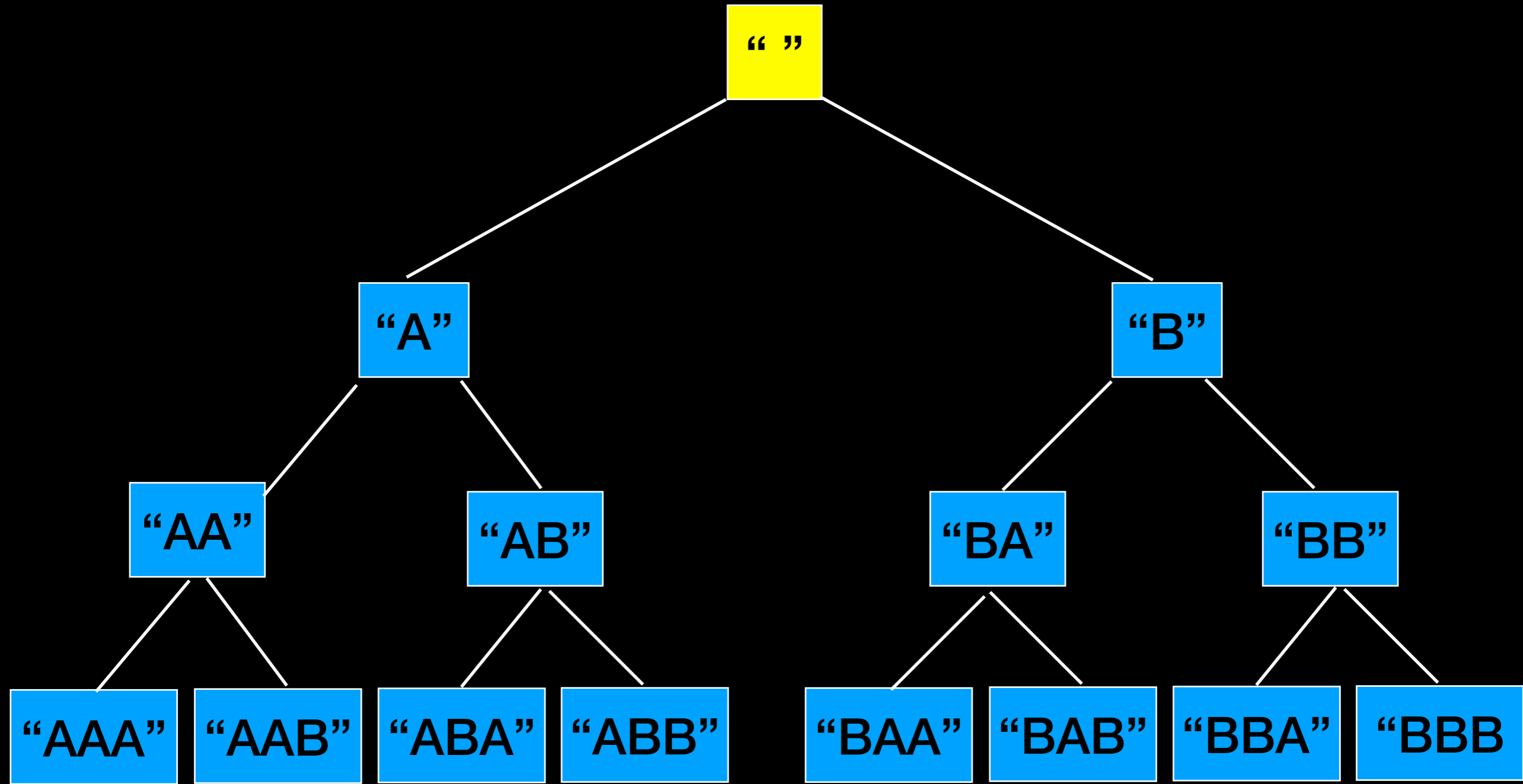
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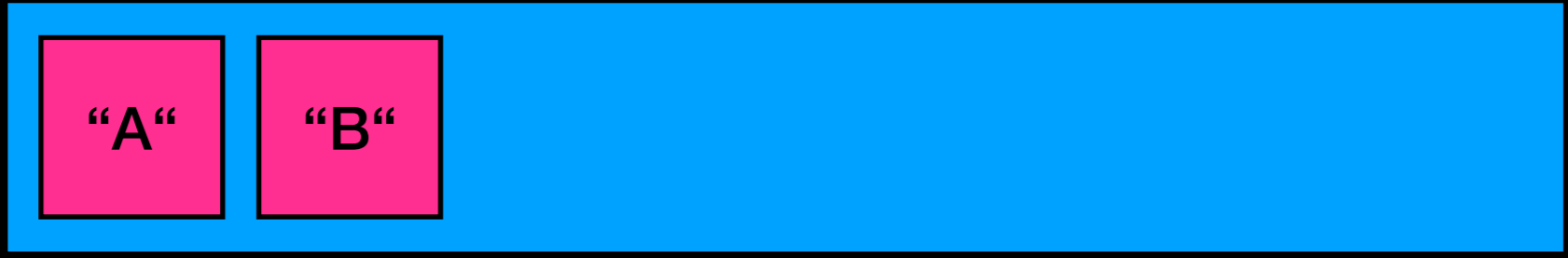
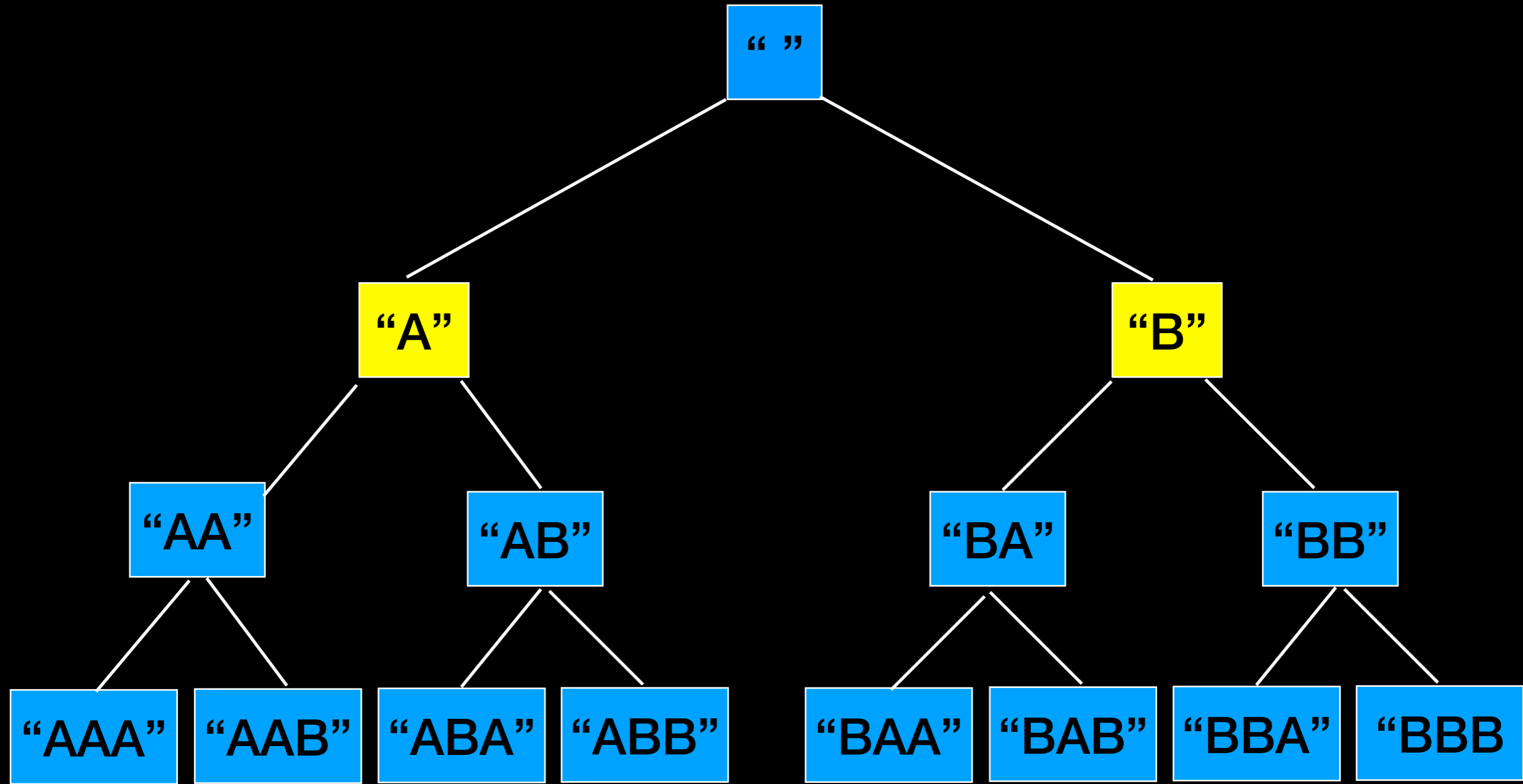
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```

$O(26^n)$

Let $n = 3$, alphabet still $\{ 'A', 'B' \}$

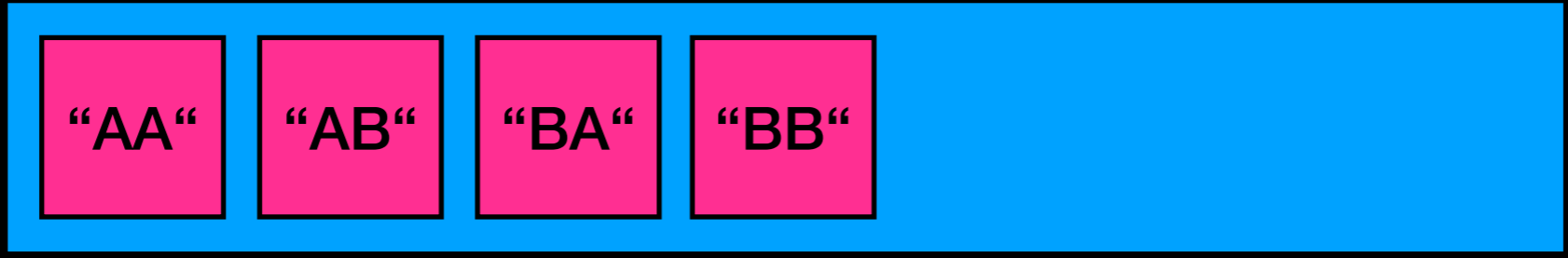
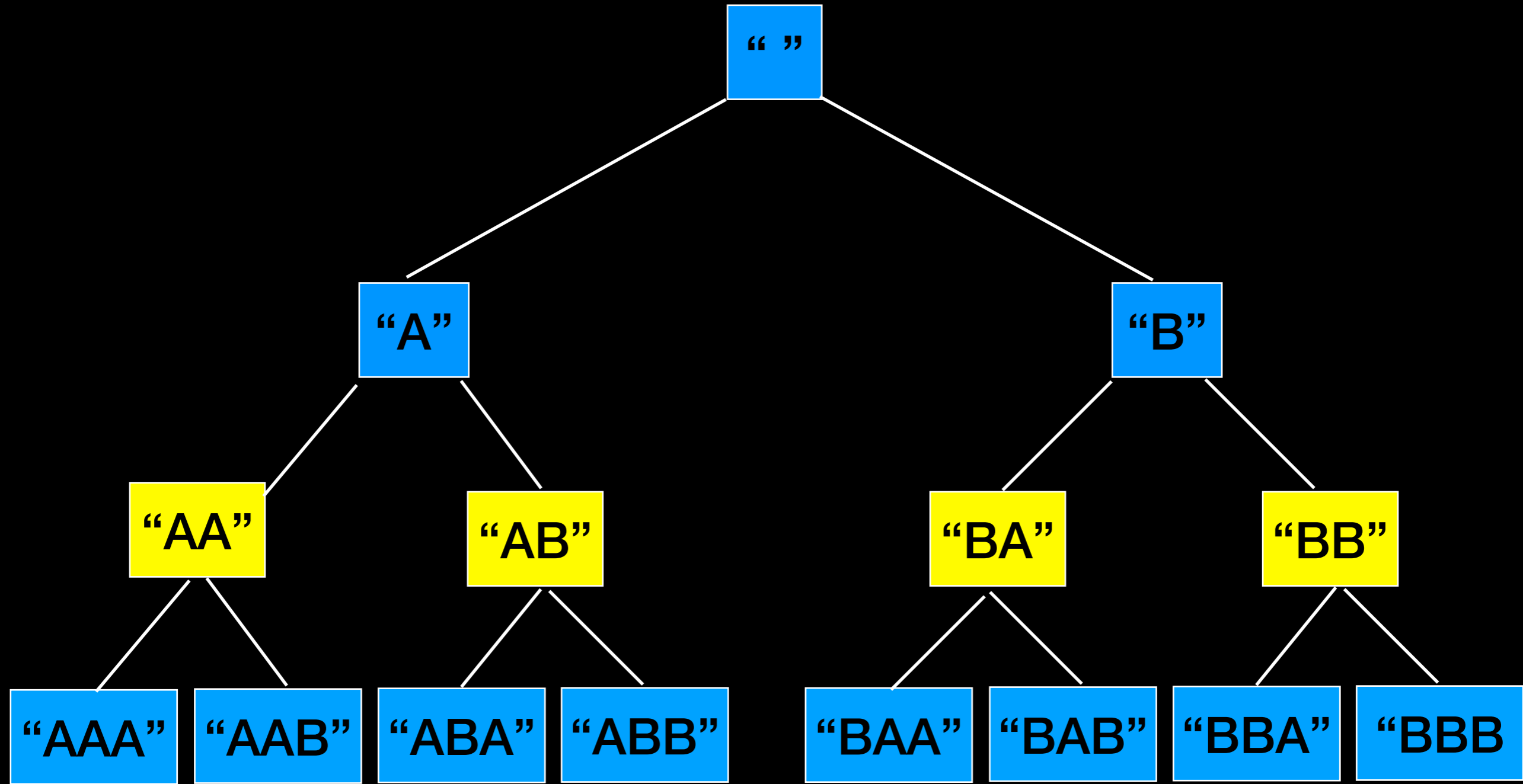


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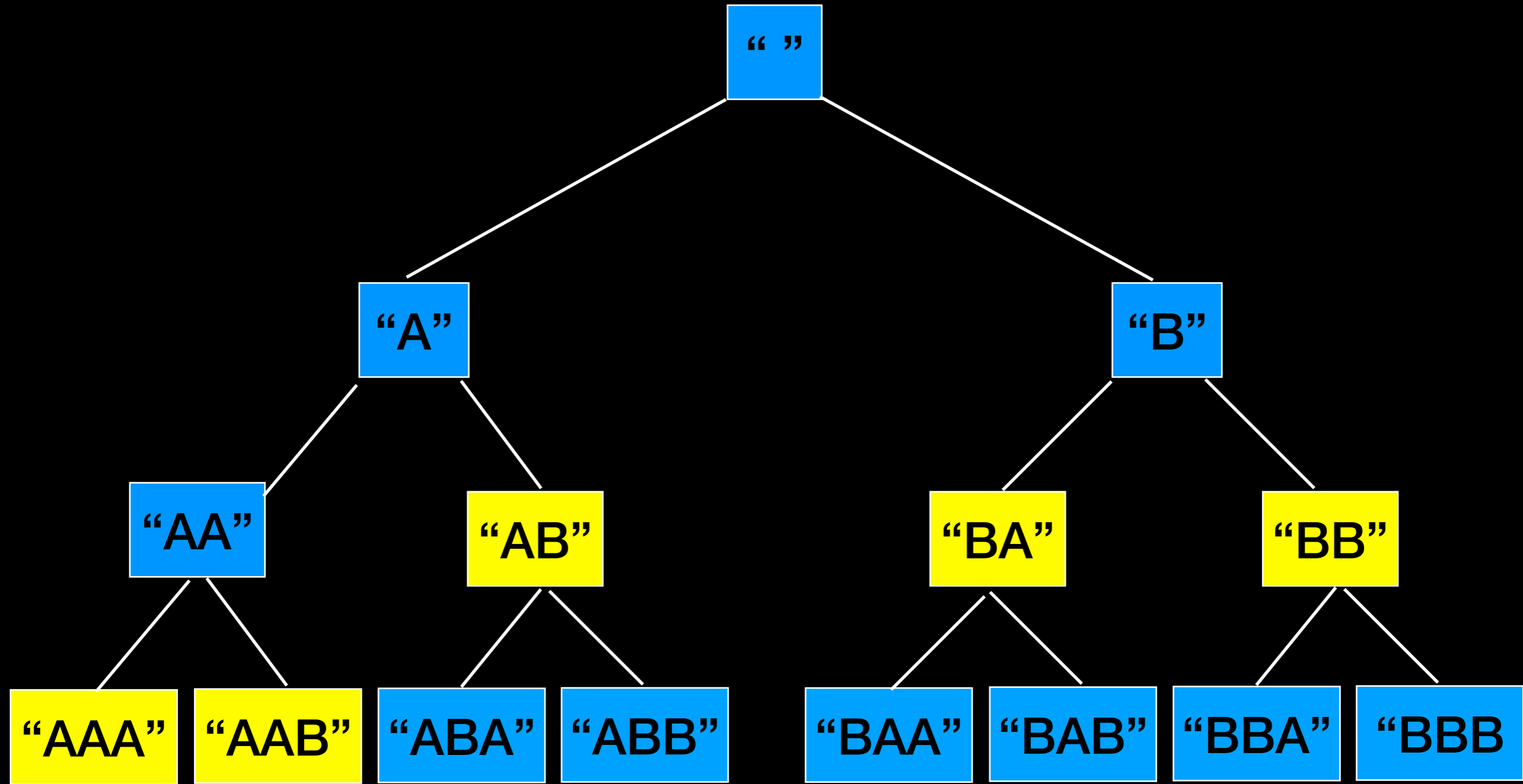
21

Let $n = 3$, alphabet still $\{ 'A', 'B' \}$



2^2

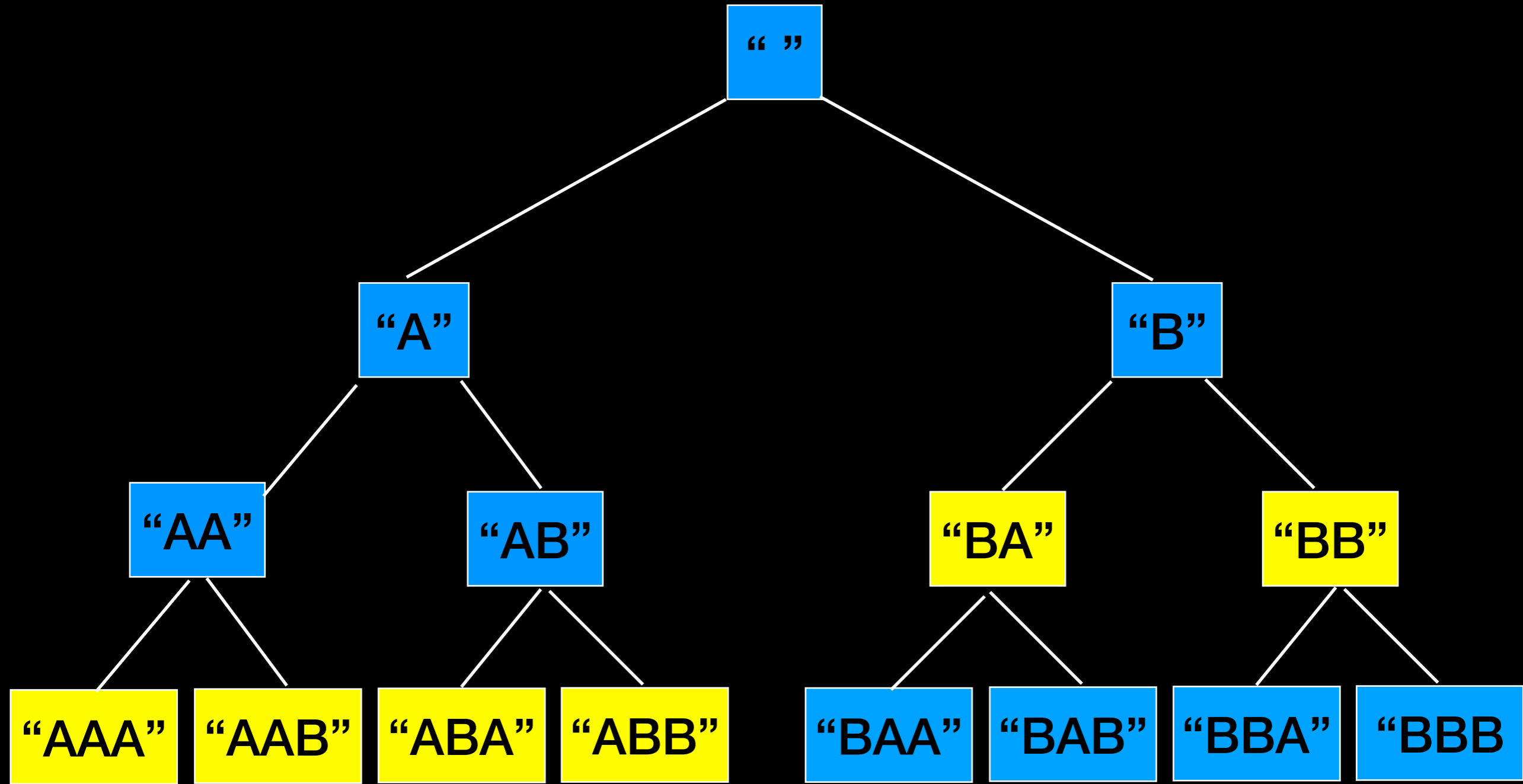
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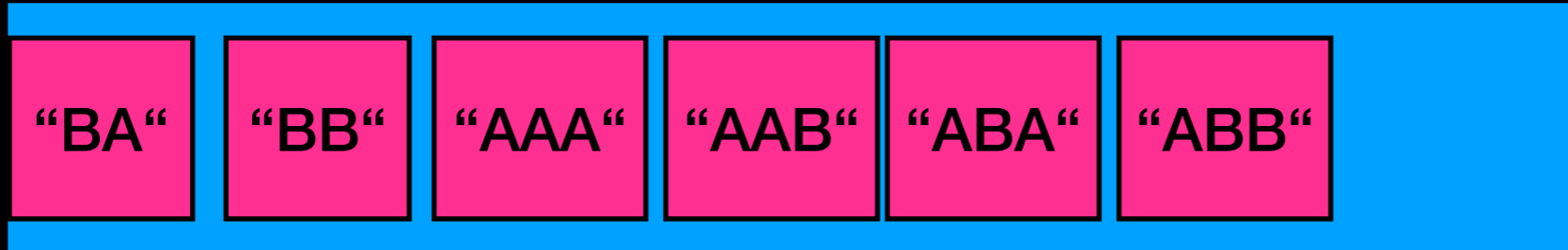
“AA”

“AB” “BA” “BB” “AAA” “AAB”

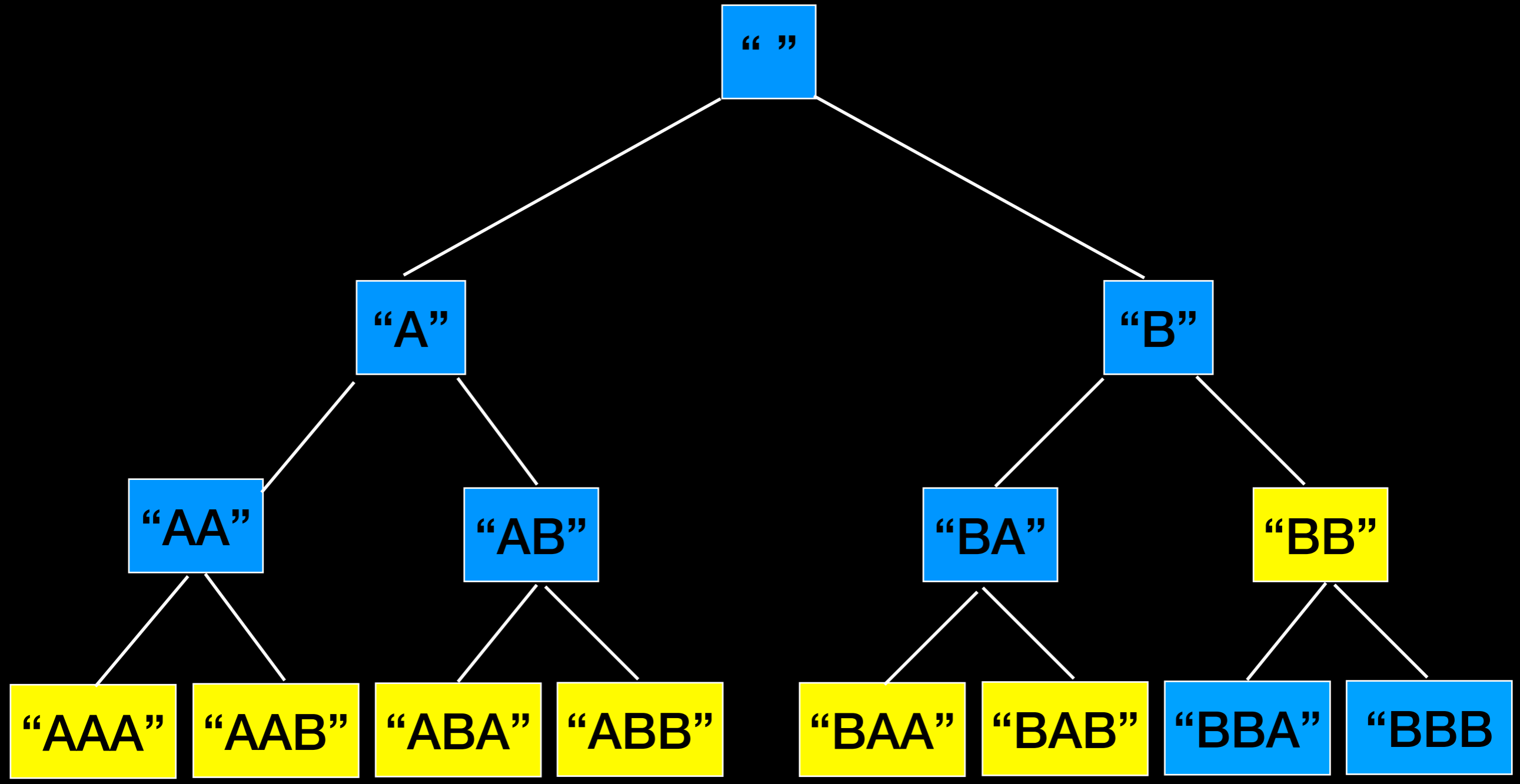
Let $n = 3$, alphabet still $\{ 'A', 'B' \}$



“AB“



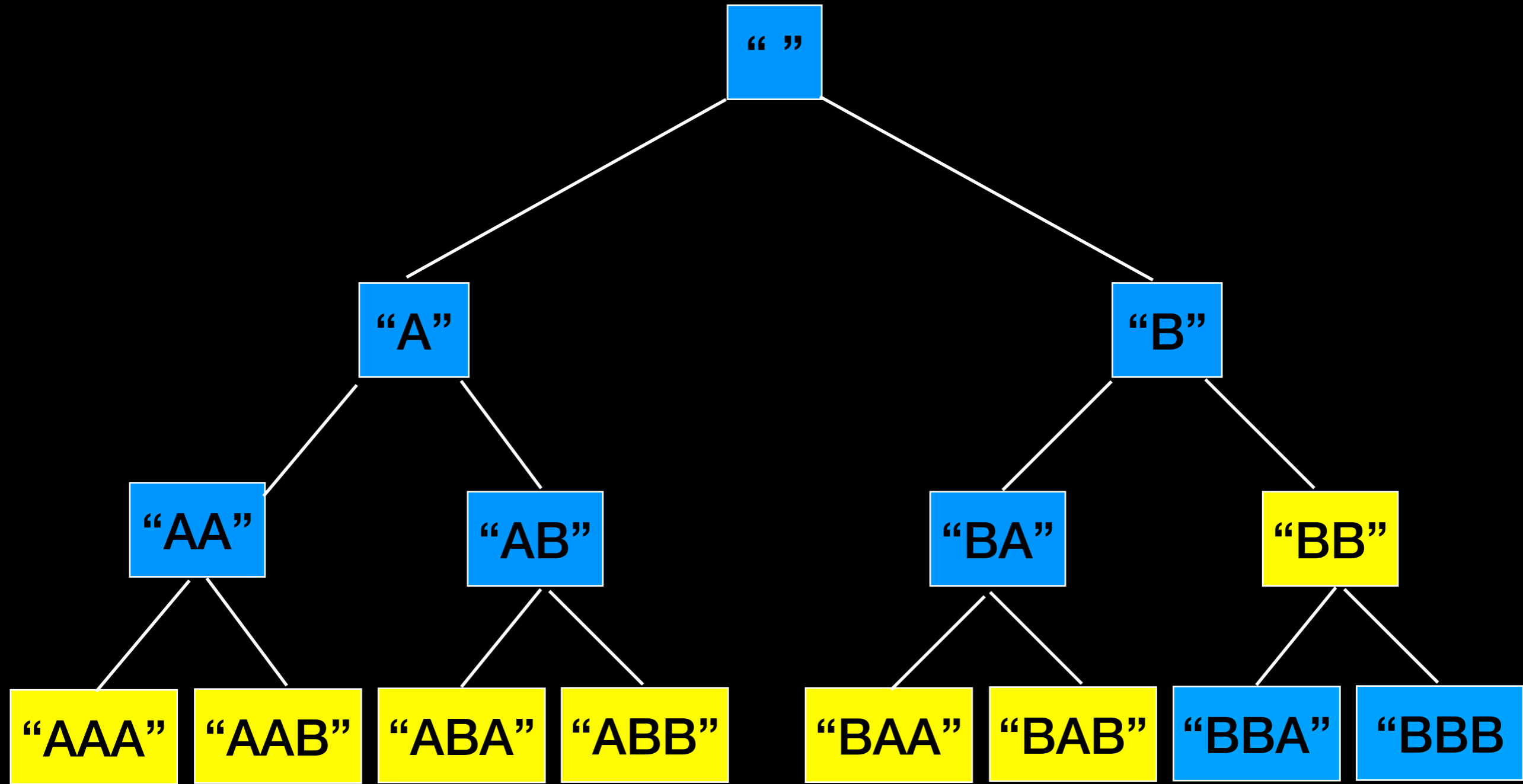
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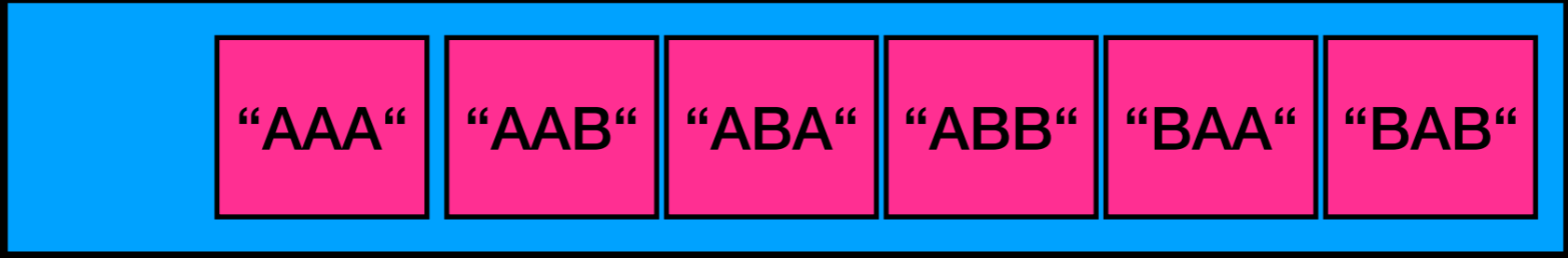
“BA“

- “BB“
- “AAA“
- “AAB“
- “ABA“
- “ABB“
- “BAA“
- “BAB“

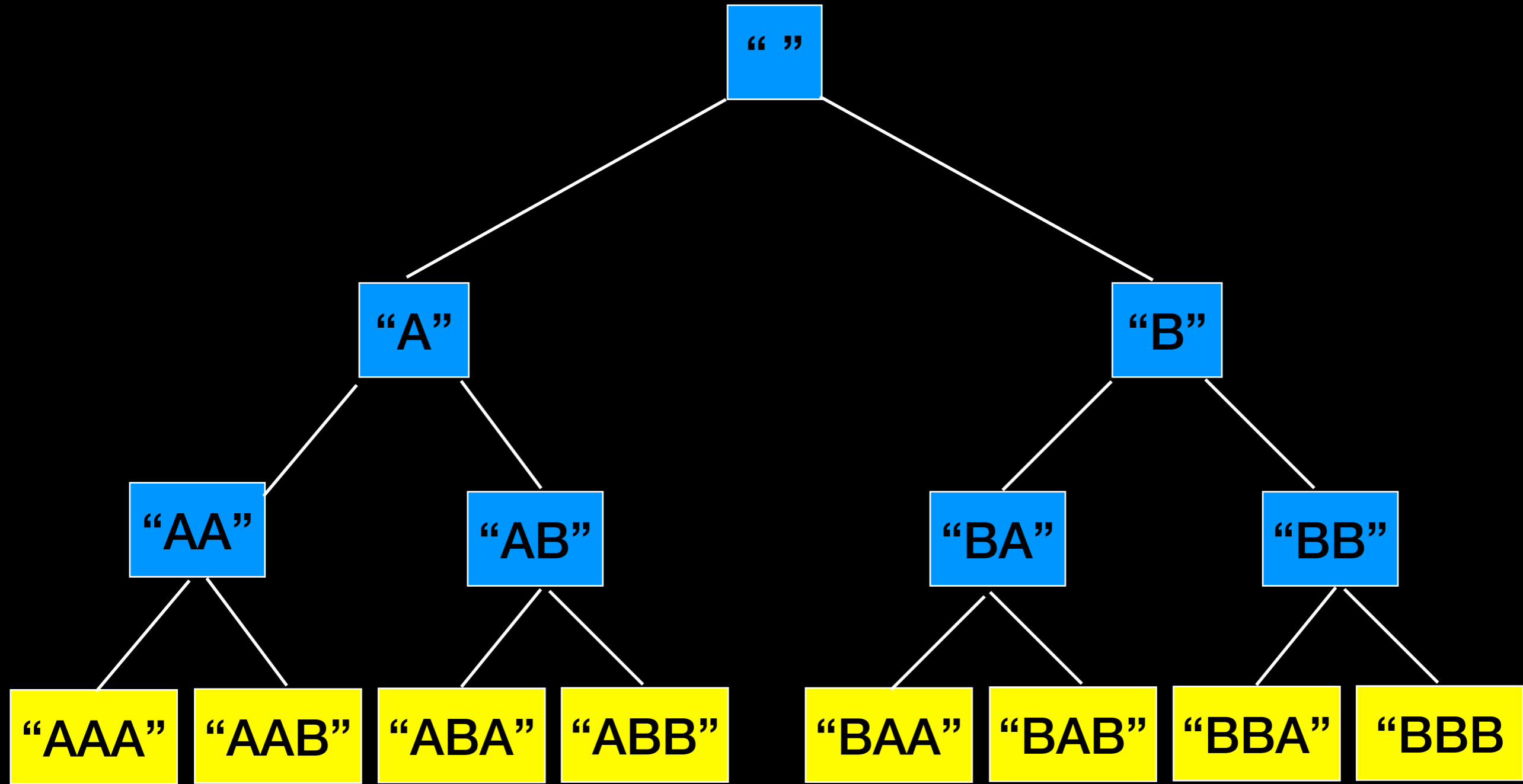
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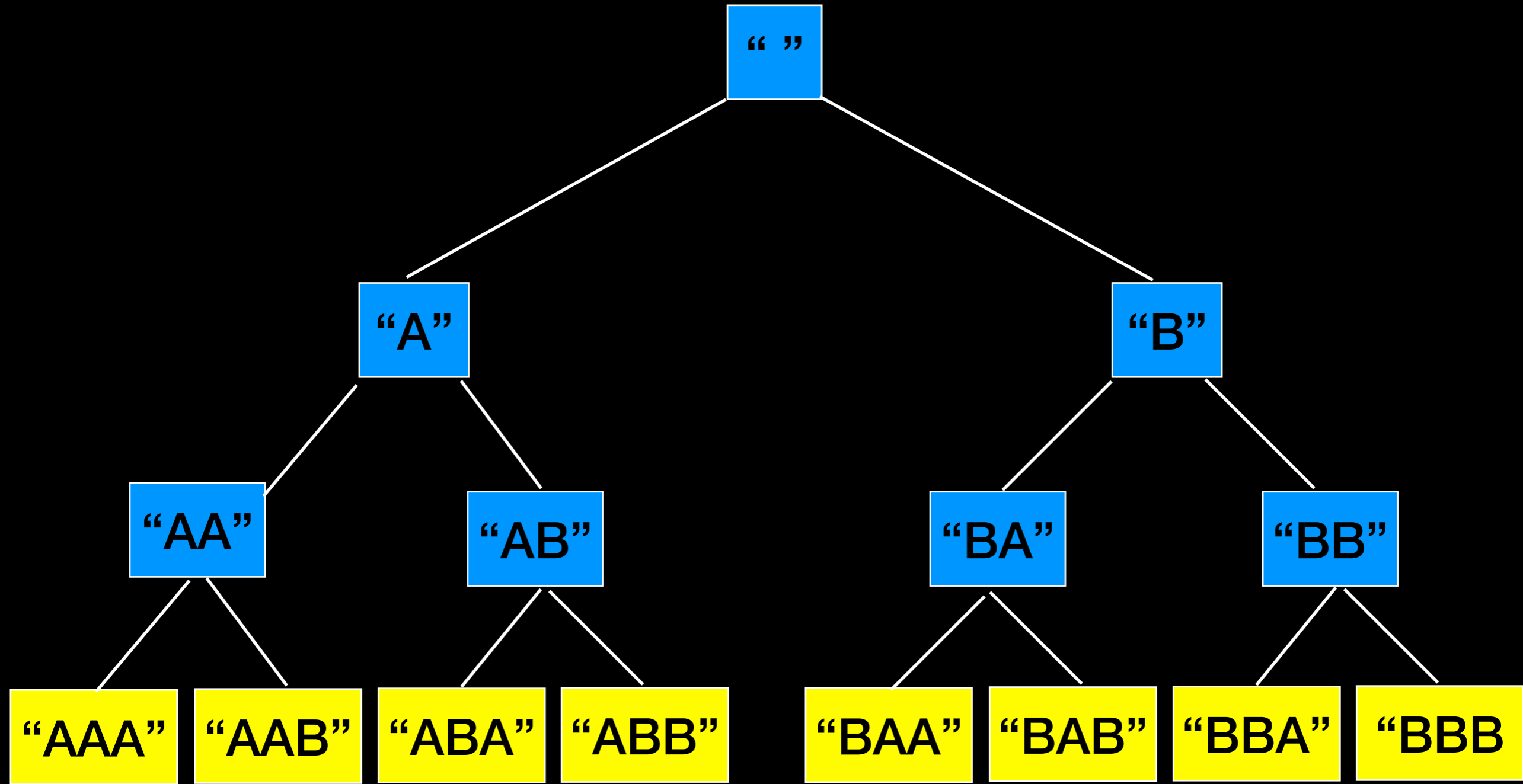
“BB”



Let $n = 3$, alphabet still $\{ 'A', 'B' \}$



Let $n = 3$, alphabet still $\{ 'A', 'B' \}$



- “AAA“
- “AAB“
- “ABA“
- “ABB“
- “BAA“
- “BAB“
- “BBA“
- “BBB“

2^3

Memory Usage

With alphabet {'A', 'B', ..., 'Z'}, at some point we end up with 26^n strings in memory

Size of string on my machine = 24 bytes

Running this algorithm for $n = 7$ ($\approx 193\text{GB}$) is the maximum that can be handled by a standard personal computer

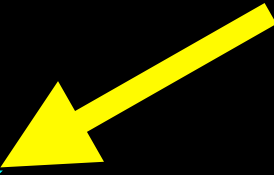
For $n = 8 \approx 5\text{TB}$



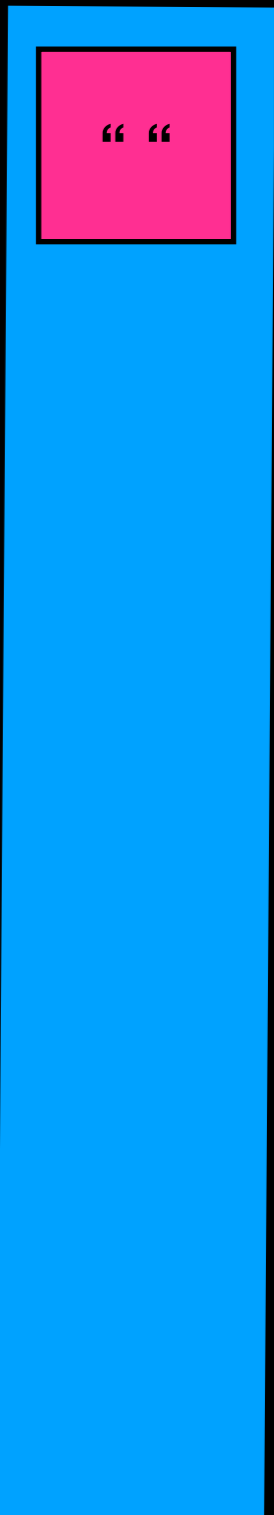
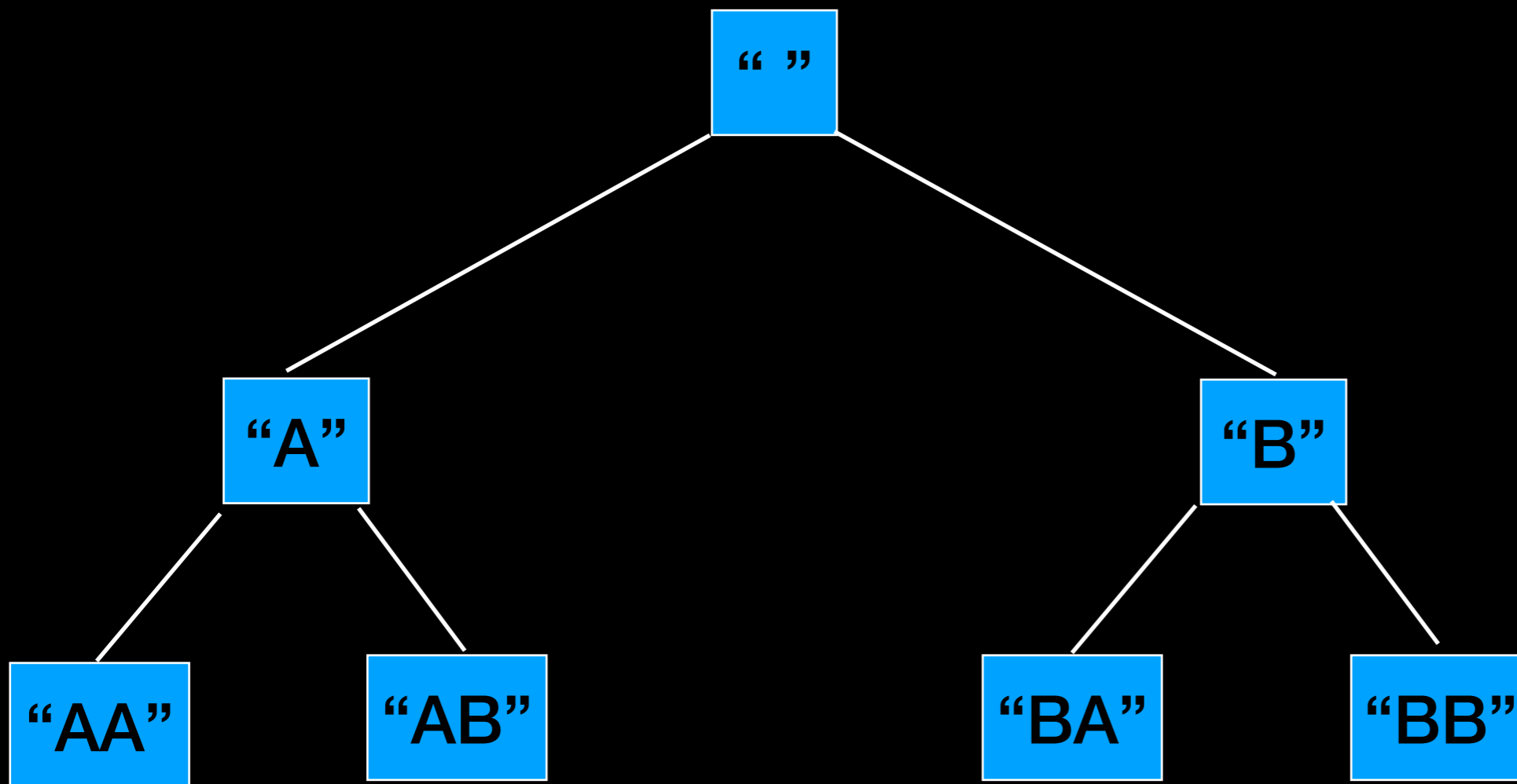
Massive
space
requirement

What if we use a stack?

```
findAllSubstrings(int n)
{
    push empty string on the stack
    while(stack is not empty){
        let current_string = pop and add to result
        if(size of current_string < n){
            for(each character ch)//every character in alphabet
                append ch to current_string and push it
        }
    }
    return result;
}
```

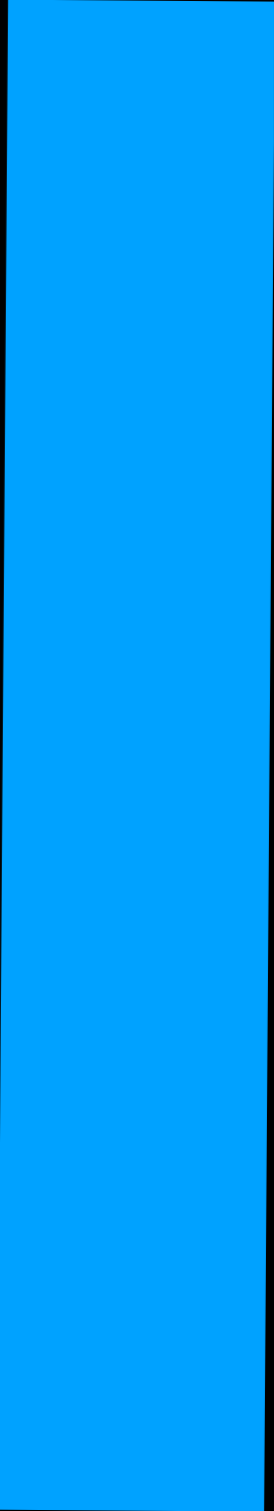
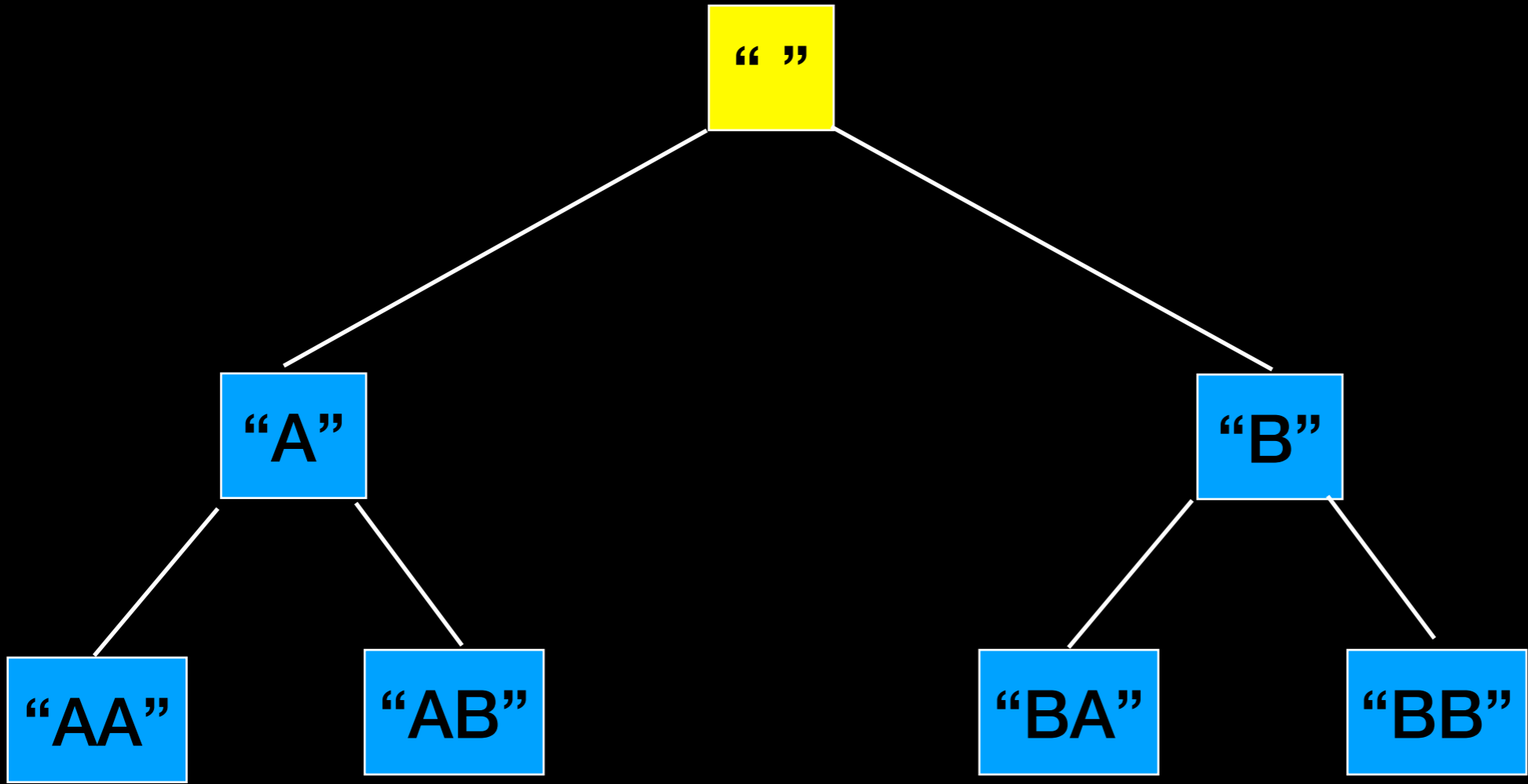


$O(26^n)$



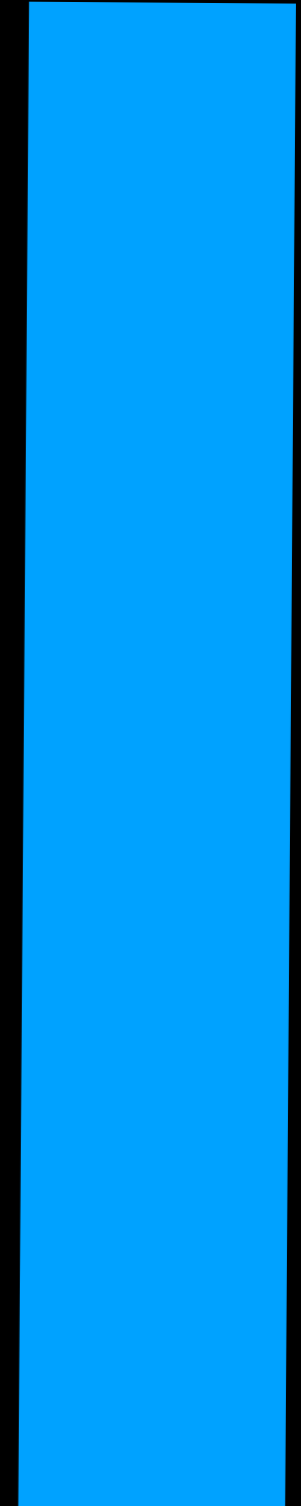
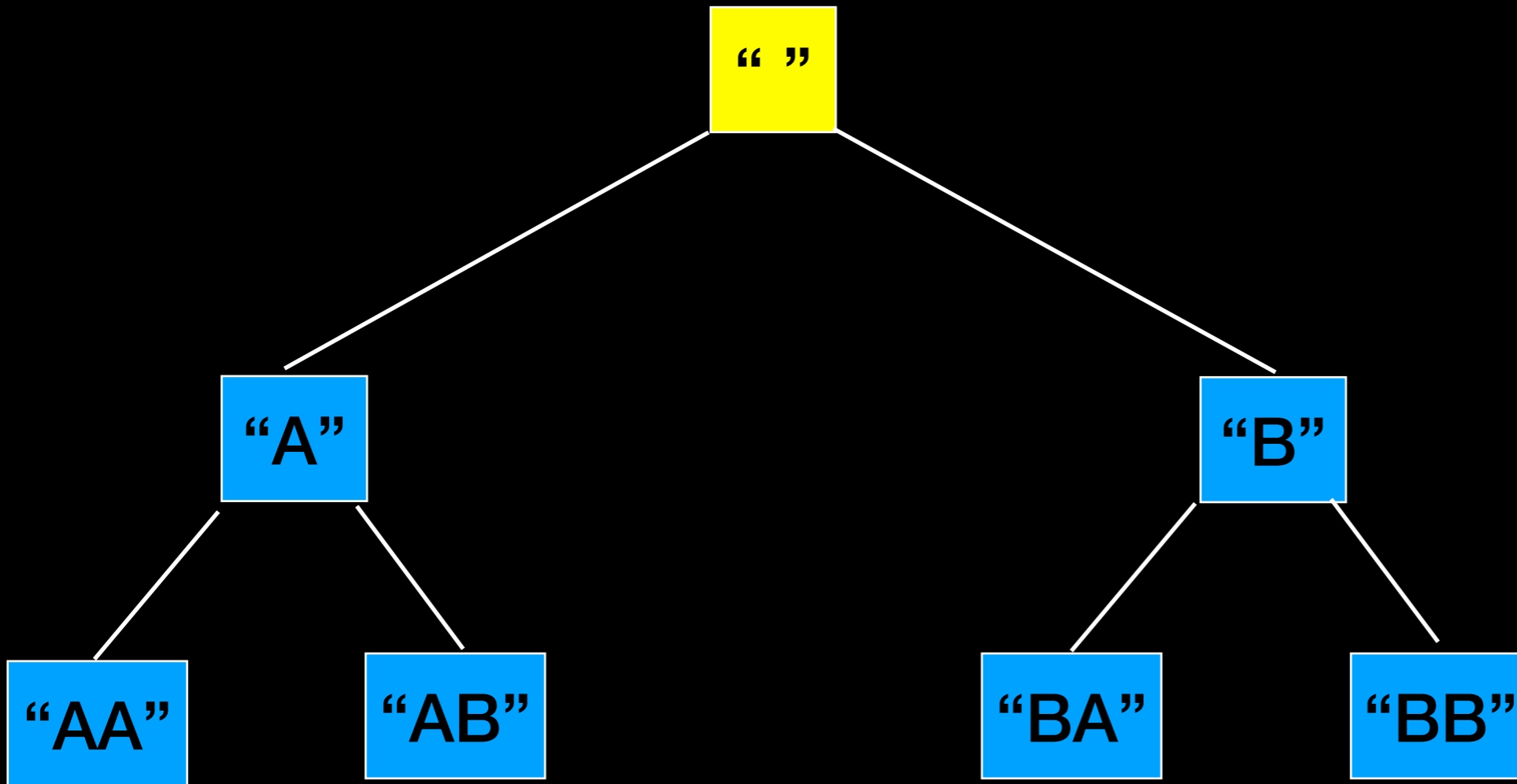
{ "" }

“ ”

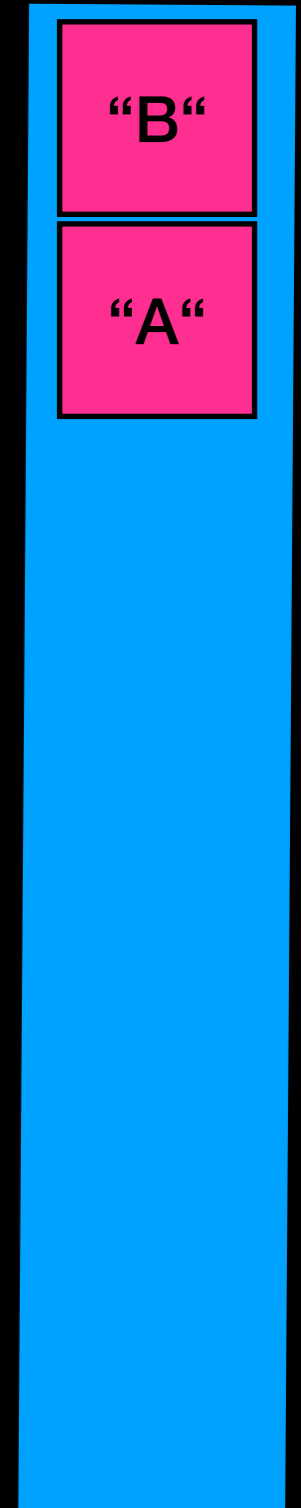
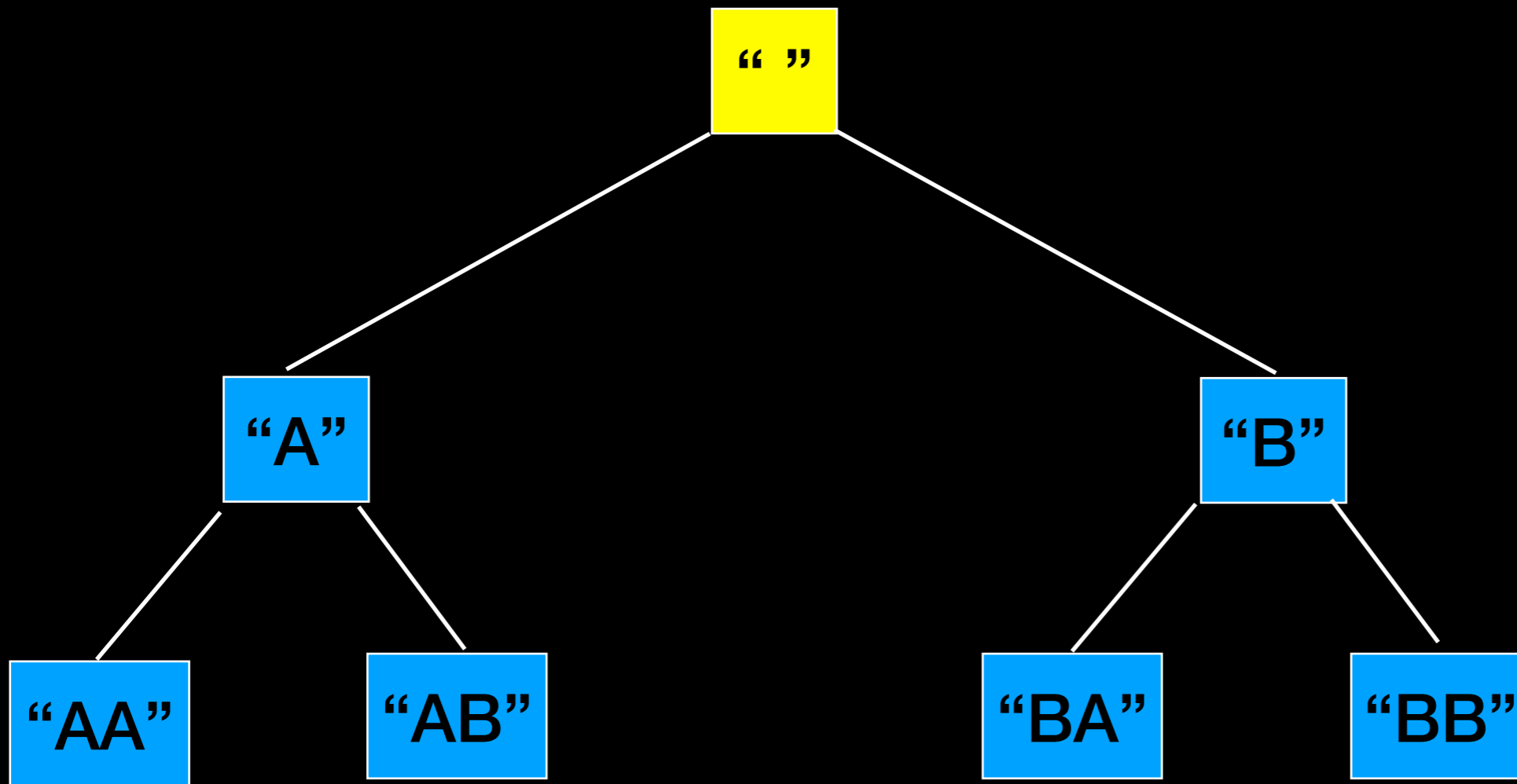


{ "" }

“ “ “A” “B”

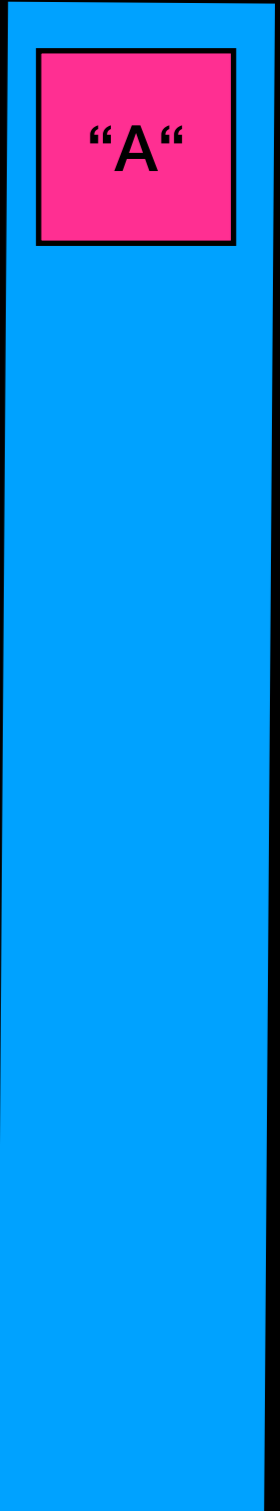
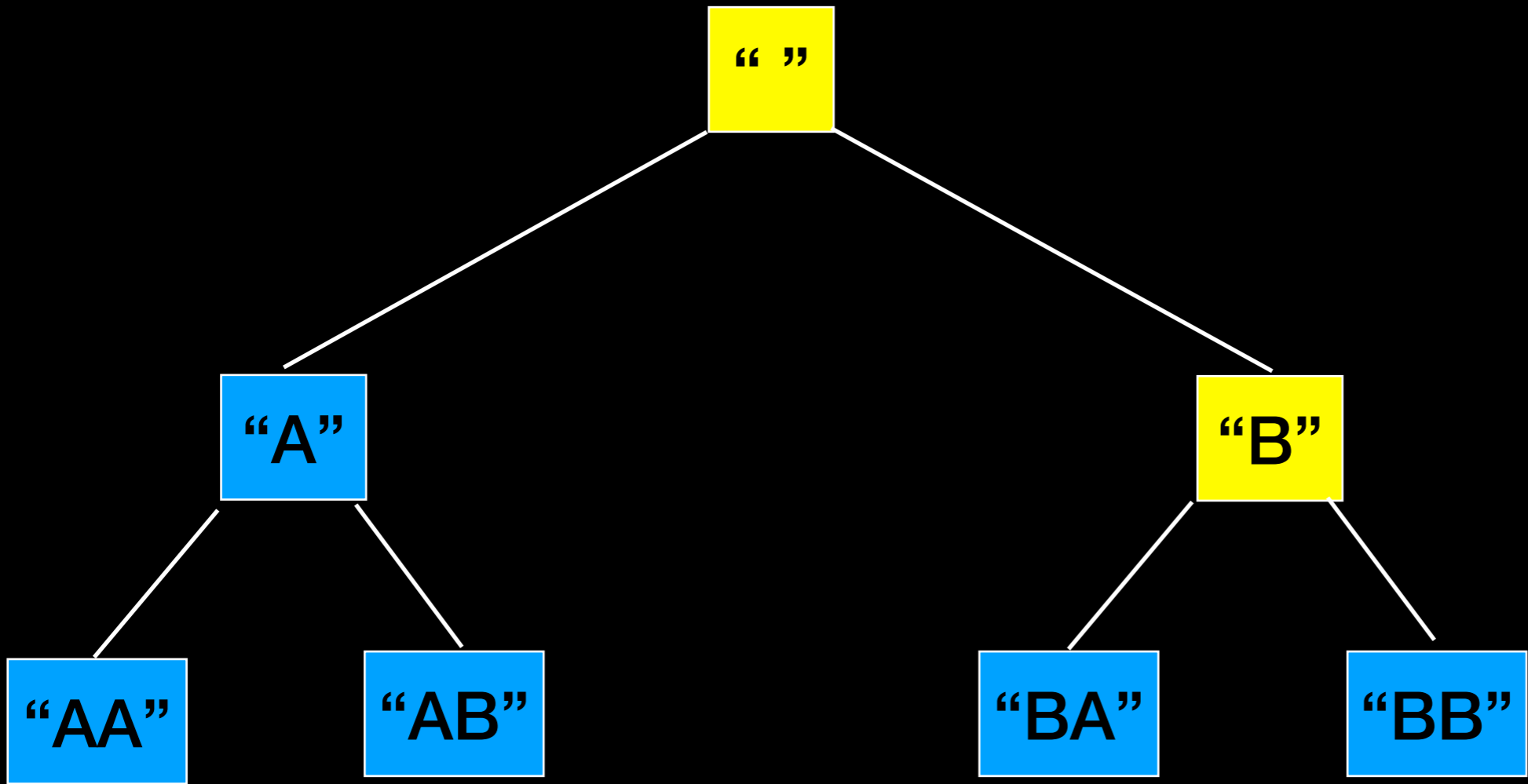


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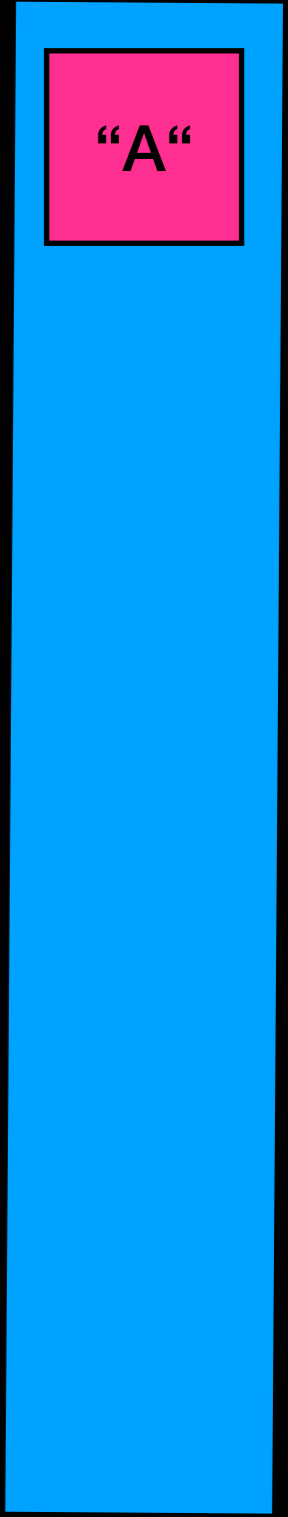
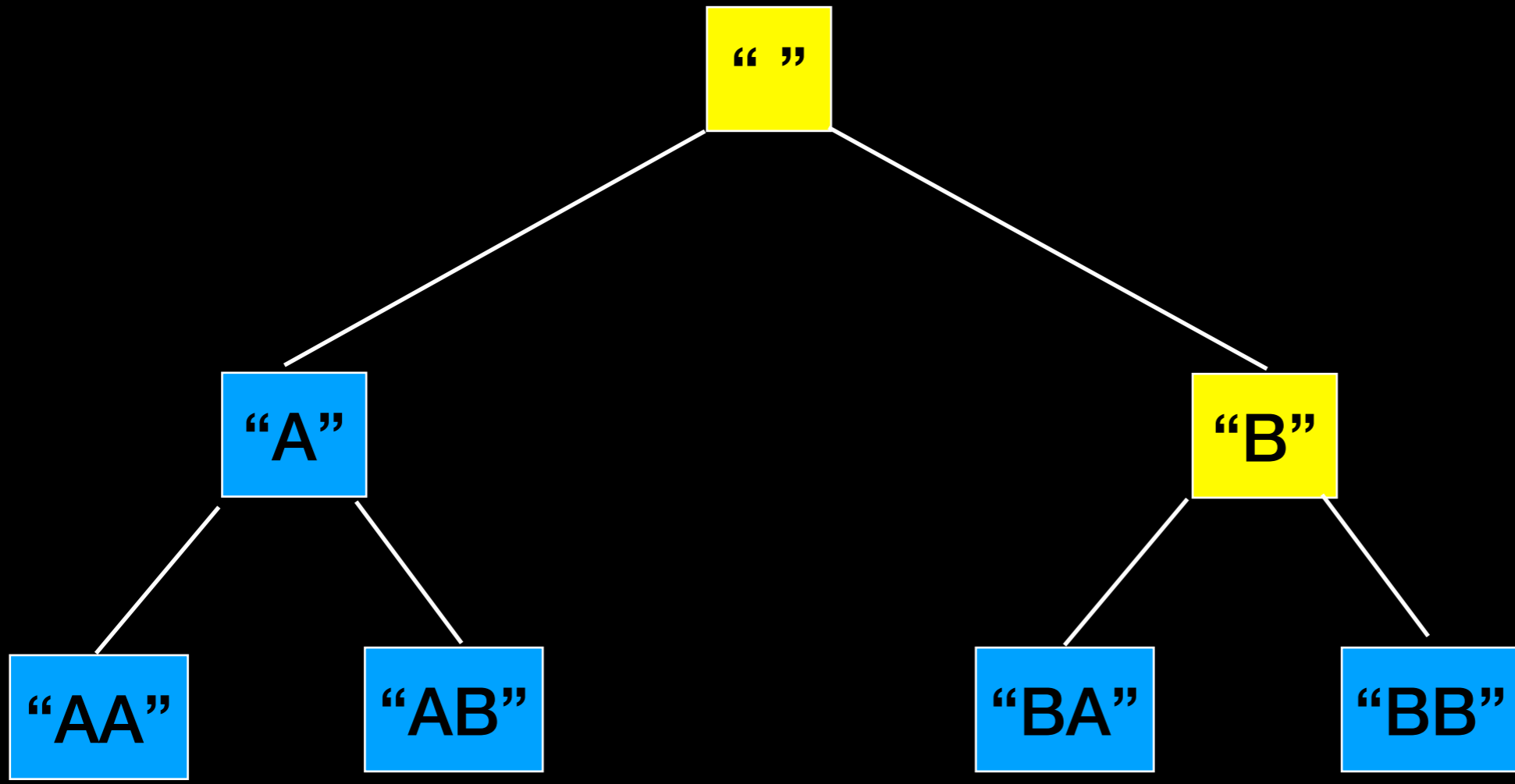
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“B”

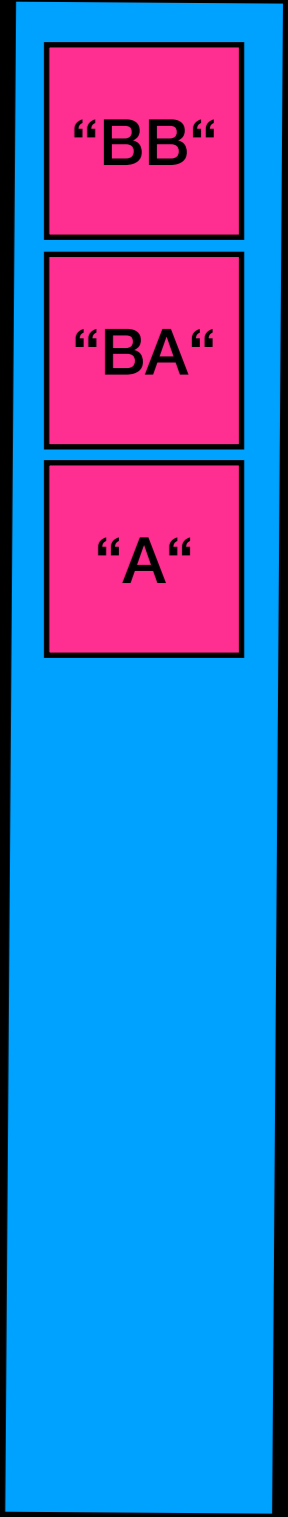
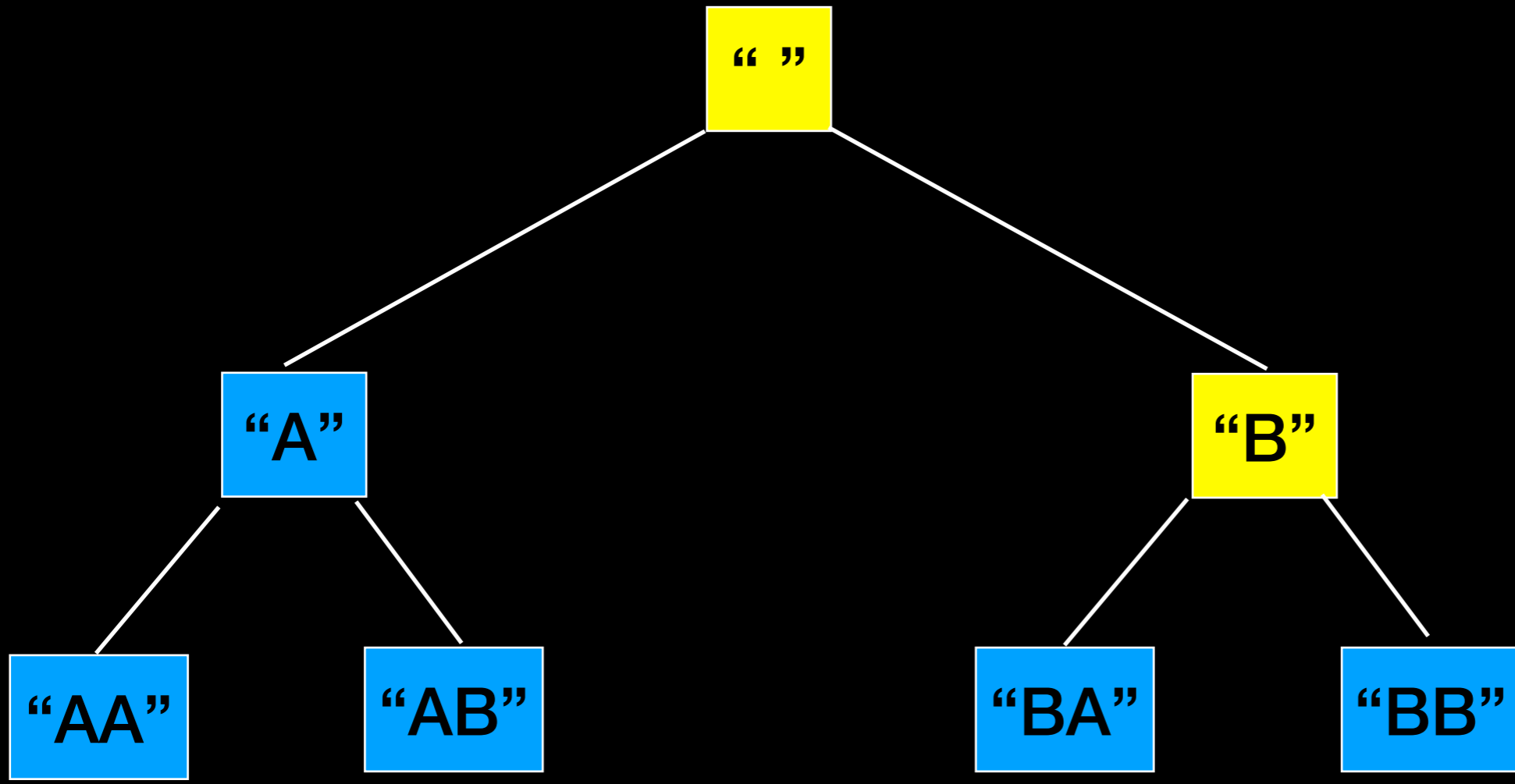


{ "", "B" }

"B" "BA" "BB"

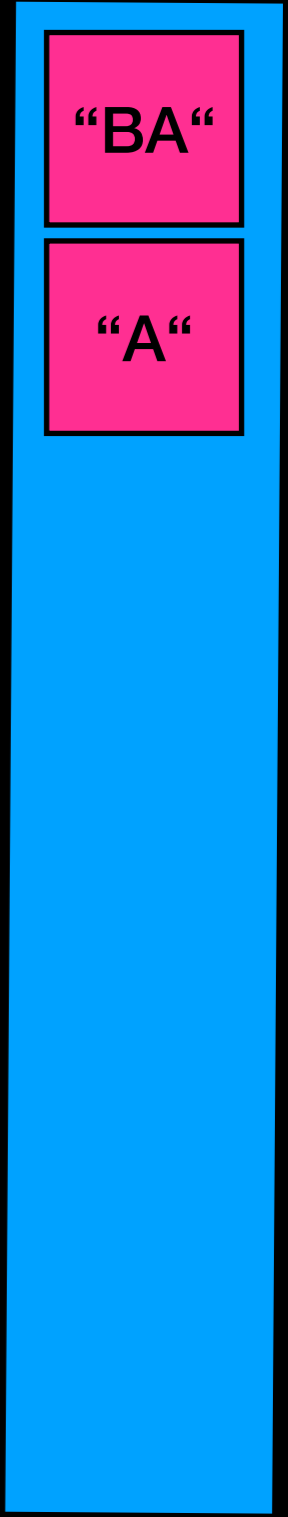
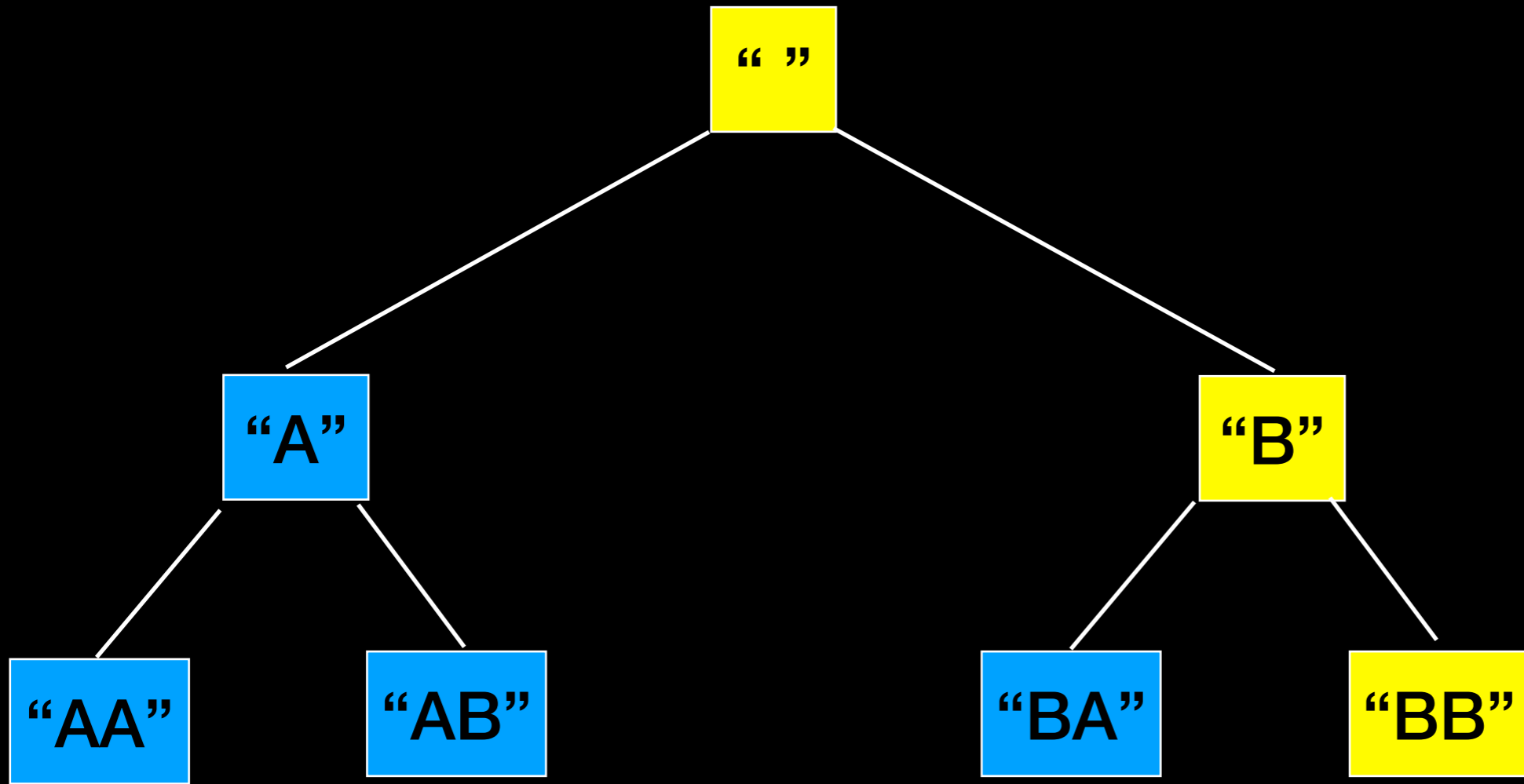


{ "", "B" }



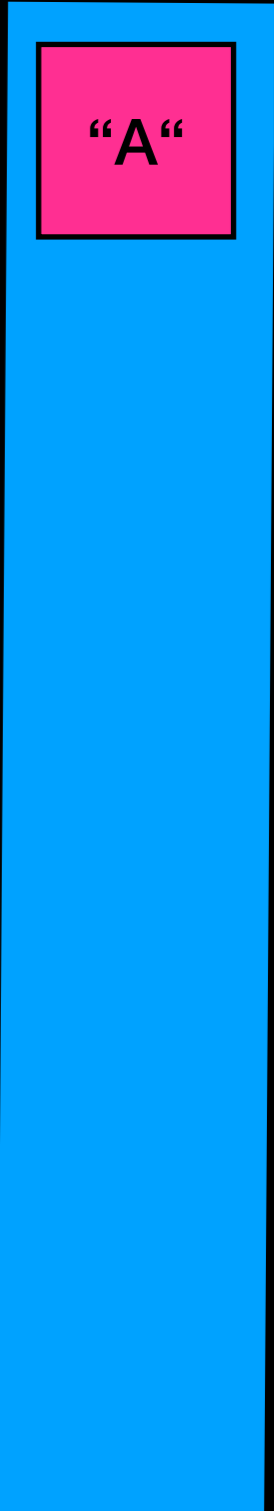
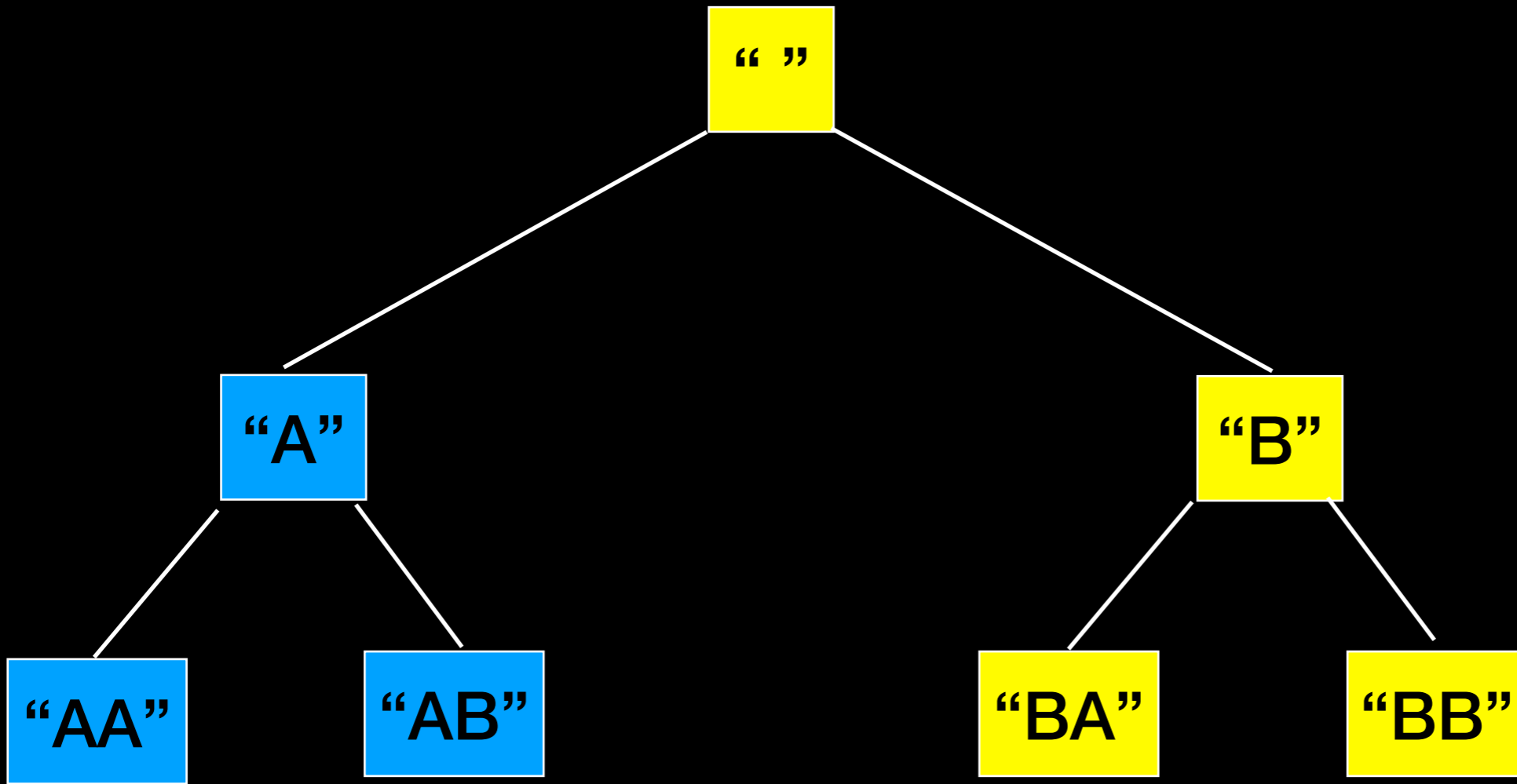
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"BB"



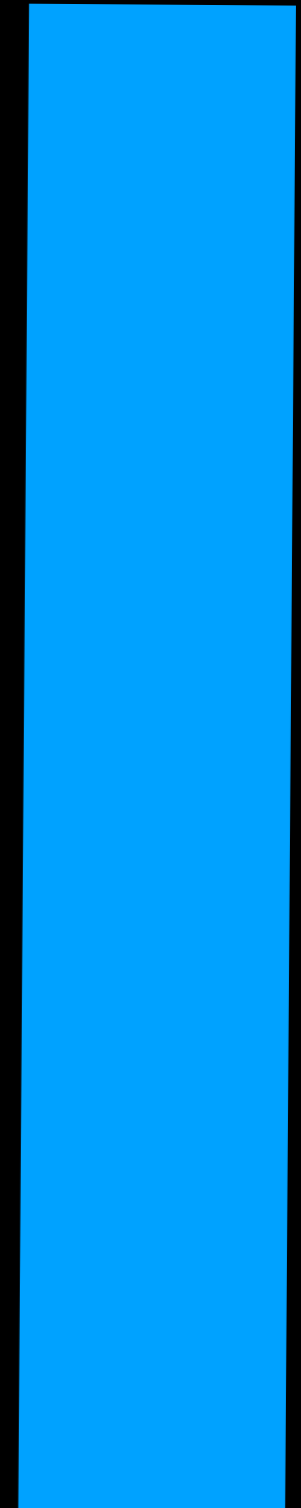
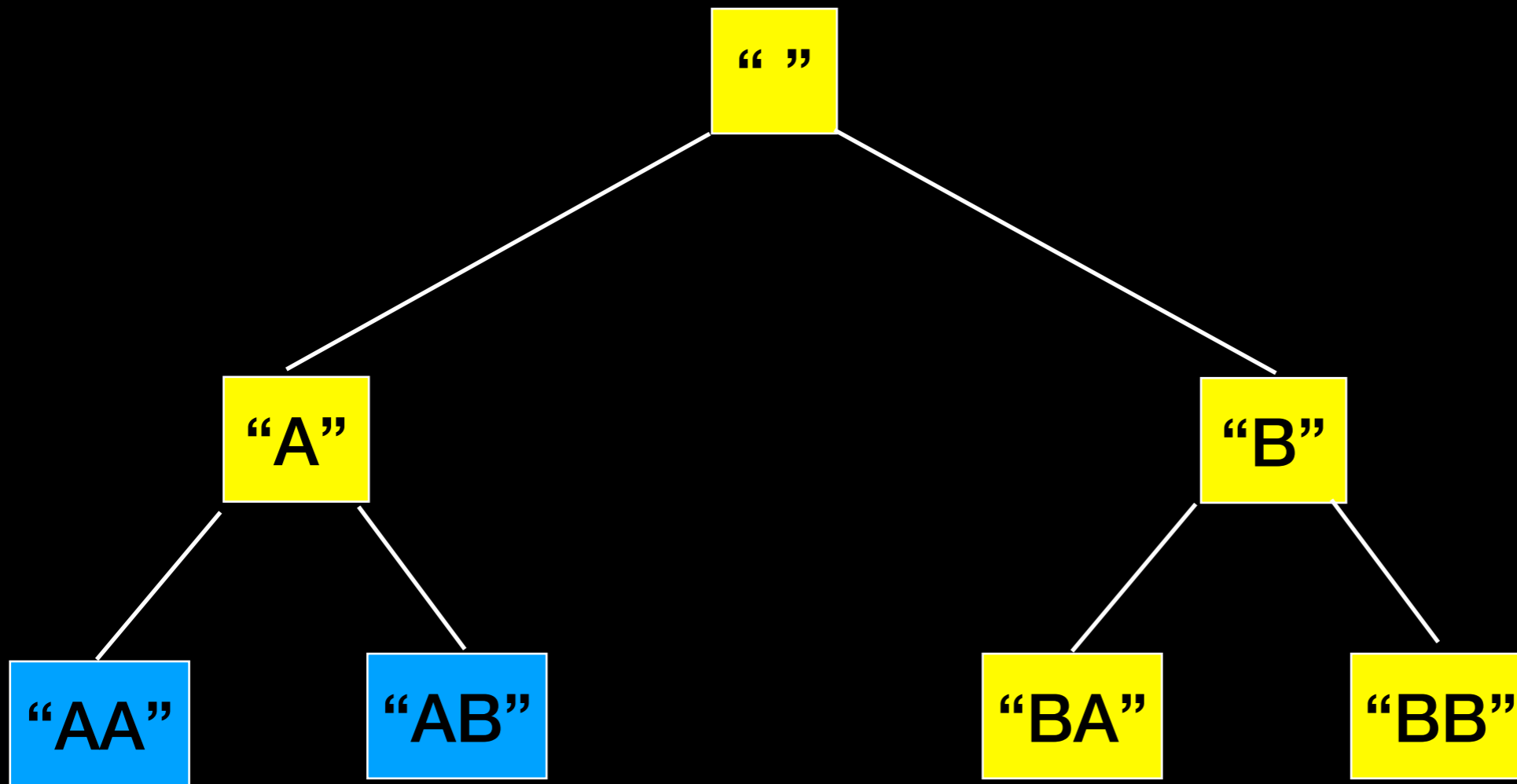
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"BA"



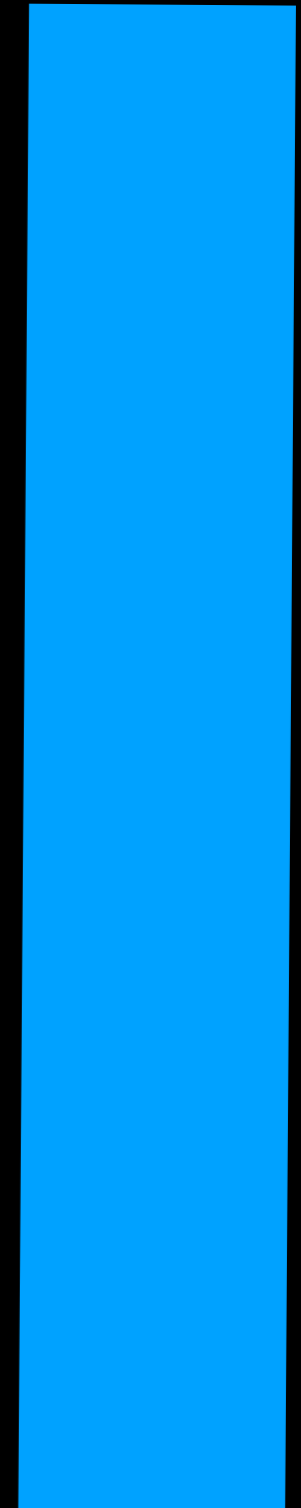
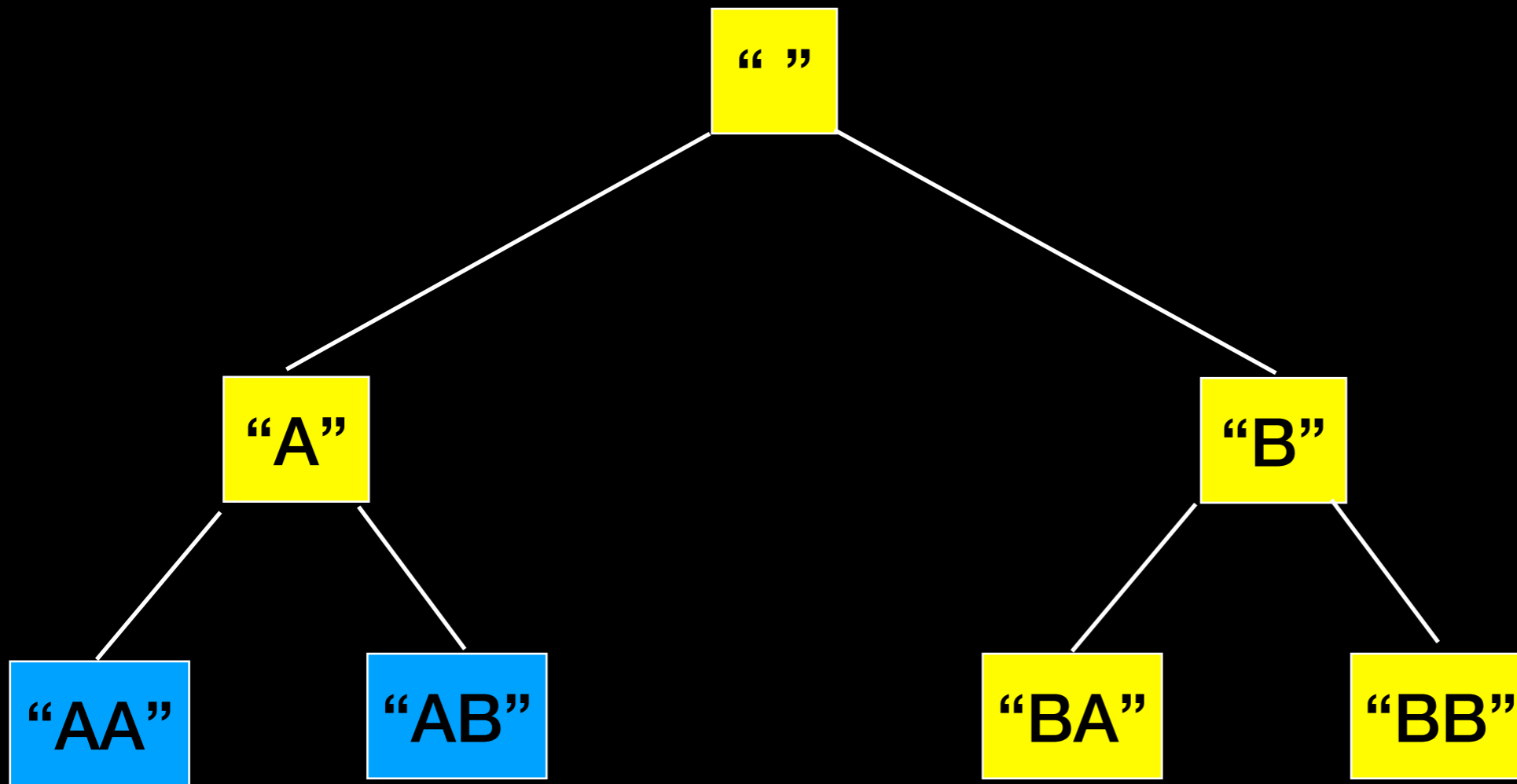
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"A"

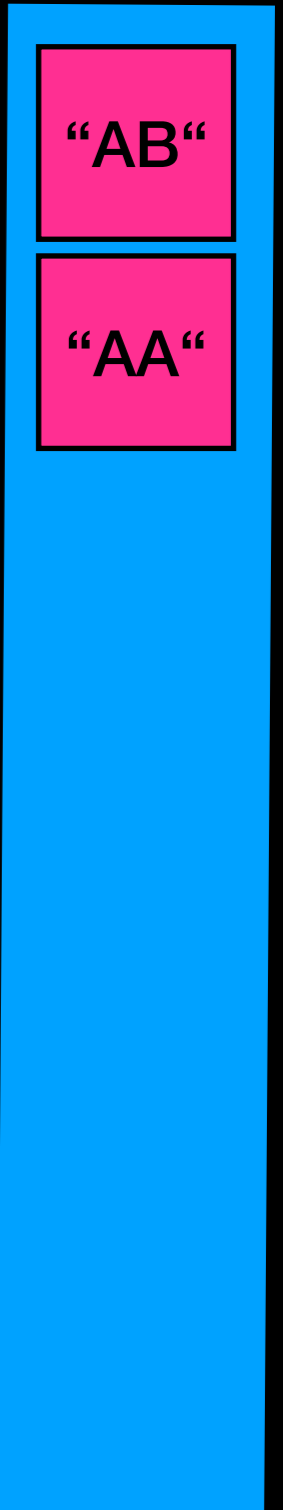
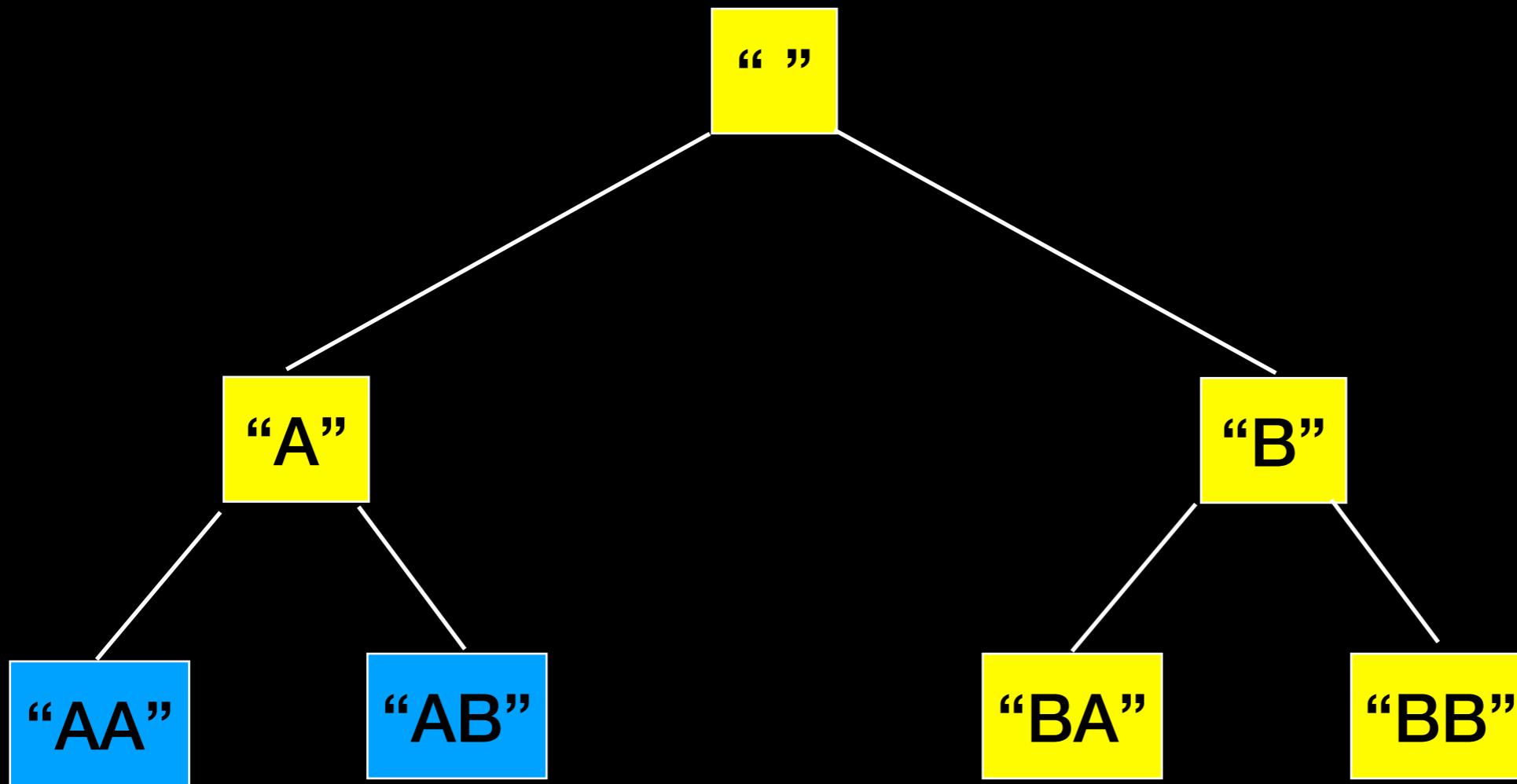


{ "", "B", "BB", "BA", "A" }

"A" "AA" "AB"

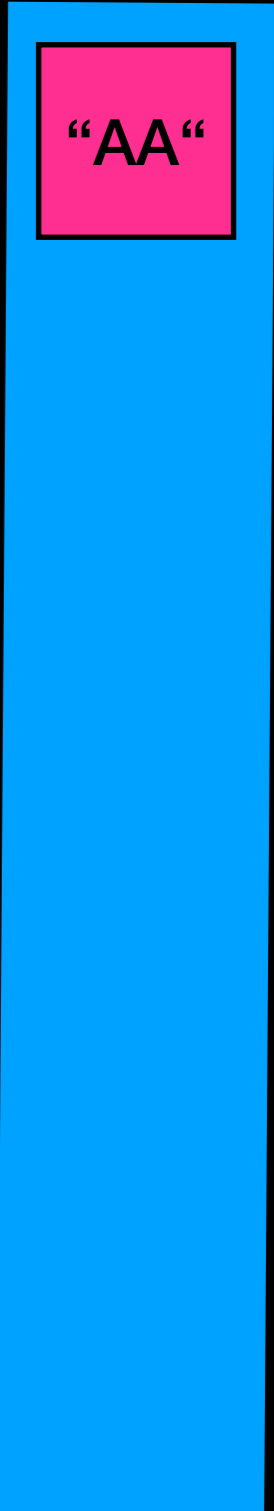
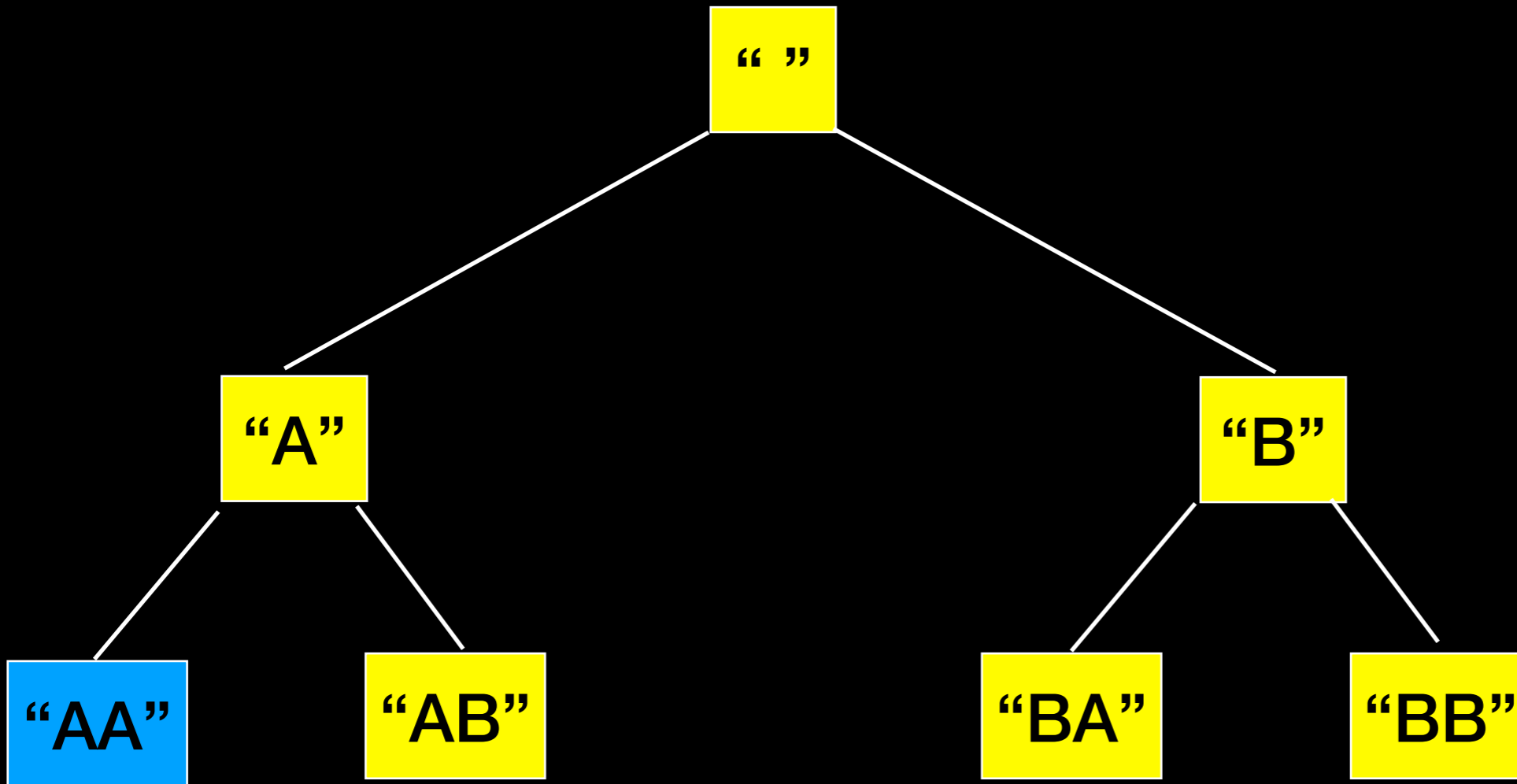


{ "", "B", "BB", "BA", "A" }



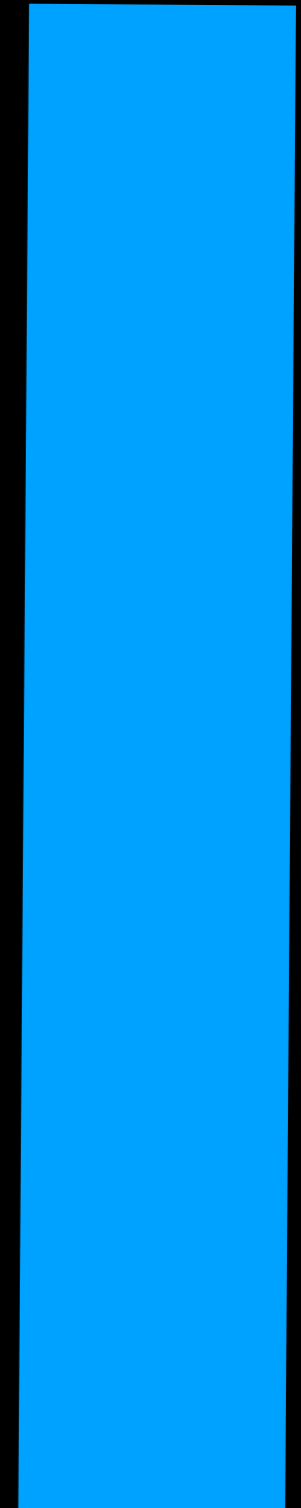
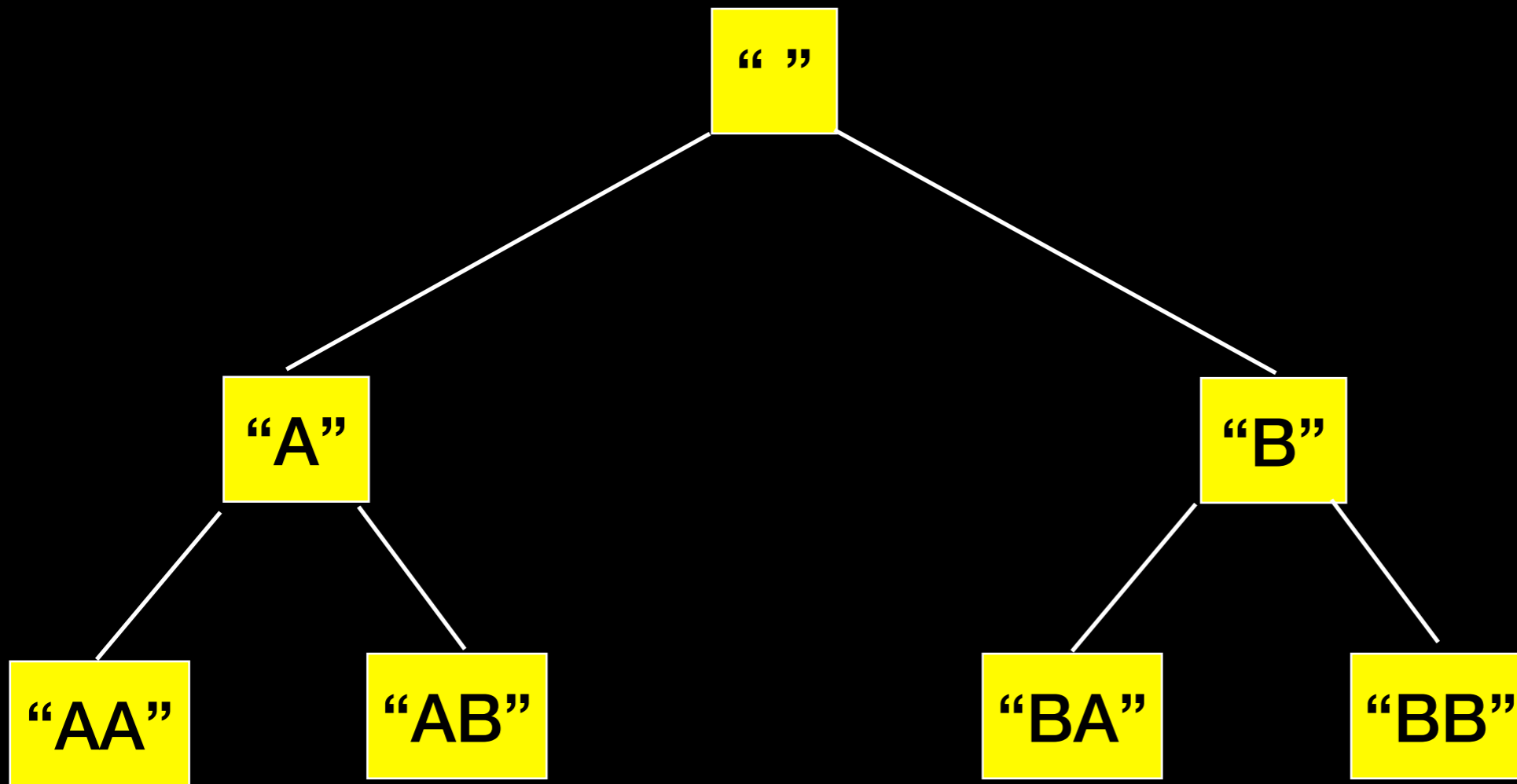
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"AB"

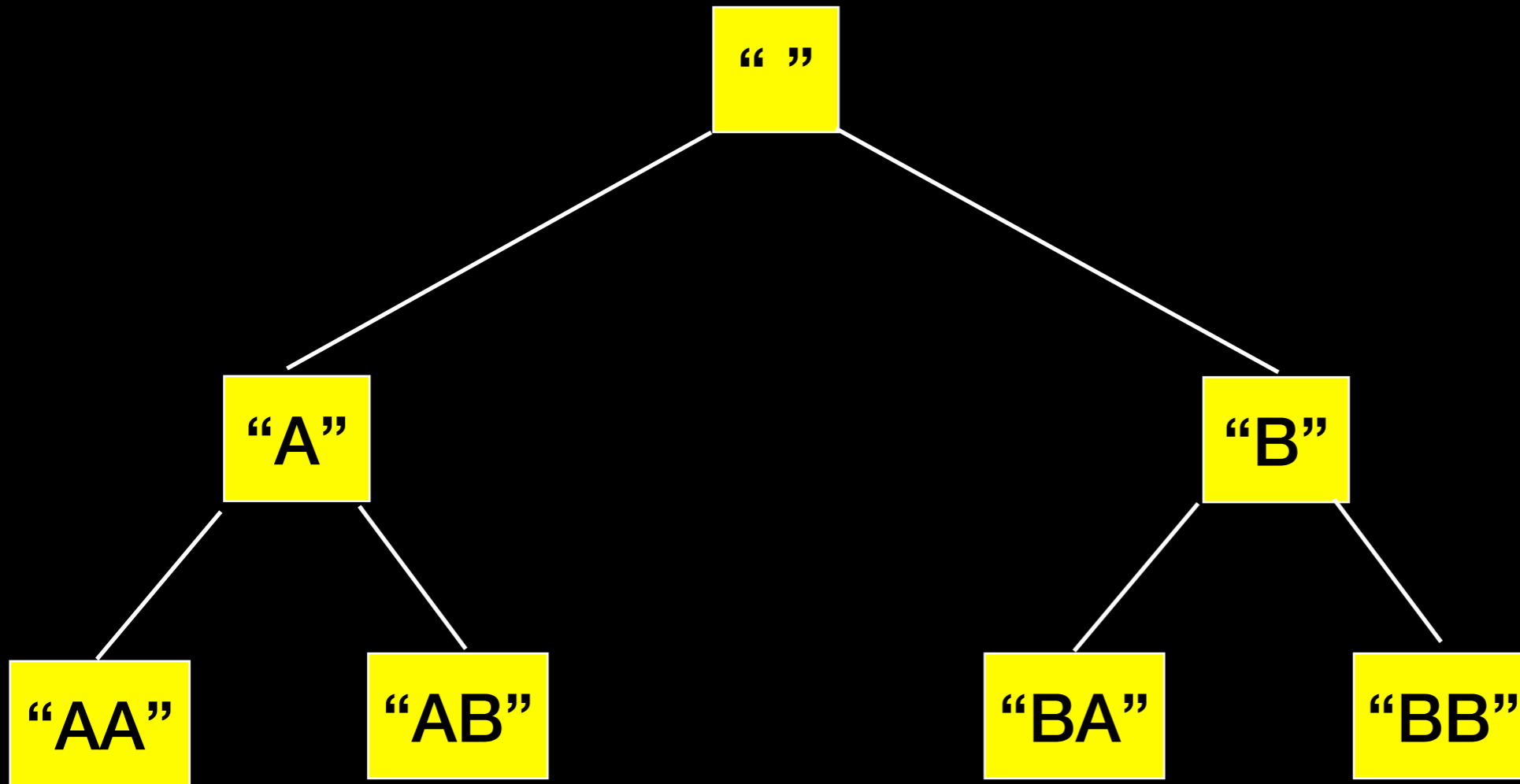


{ "", "B", "BB", "BA", "A", "AB", "AA" }

"AA"



{ "", "B", "BB", "BA", "A", "AB", "AA" }



What's the difference?

Depth-First Search

Applications

Detecting cycles in graphs

Path finding

Finding strongly connected components in graph

...

Same worst-case runtime analysis

More space efficient than previous approach

Does not explore options in increasing order of size

Comparison

Breadth-First Search
(using a queue)

Time $O(26^n)$

Space $O(26^n)$

Good for exploring options in increasing order of size when expecting to find "shallow" or "short" solution

Memory inefficient when must keep each "level" in memory

Depth-First Search
(using a stack)

Time $O(26^n)$

Space $O(n)$

Explores each option individually to max size - does NOT list options by increasing size

More memory efficient

Other ADTs

Deque

Double ended queue (deque)

Can add and remove to/from front and back



Deque

Double ended queue (deque)

Can add and remove to/from front and back



Deque

Double ended queue (deque)

Can add and remove to/from front and back



Deque

Double ended queue (deque)

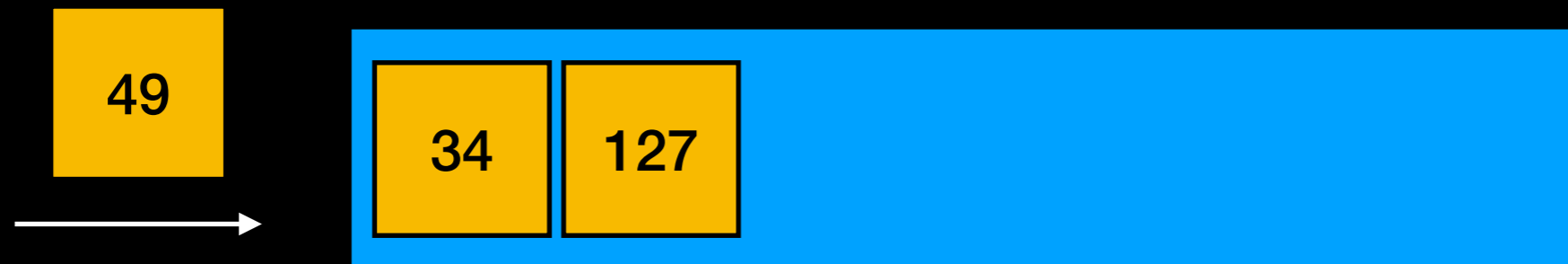
Can add and remove to/from front and back



Deque

Double ended queue (deque)

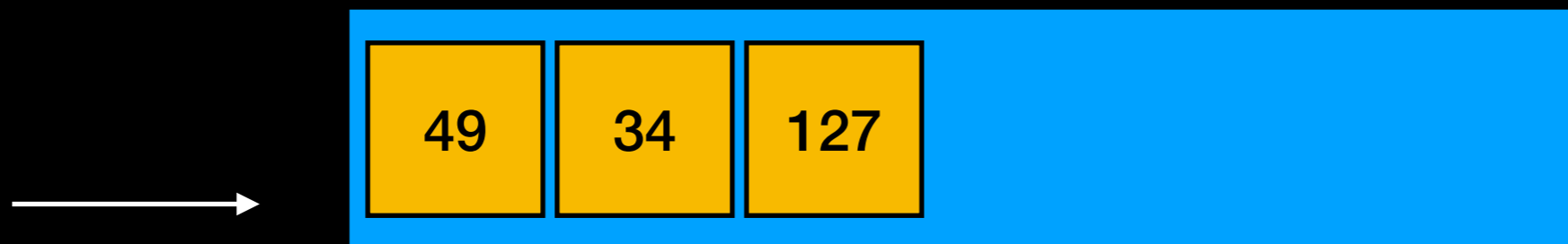
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Double ended queue (deque)

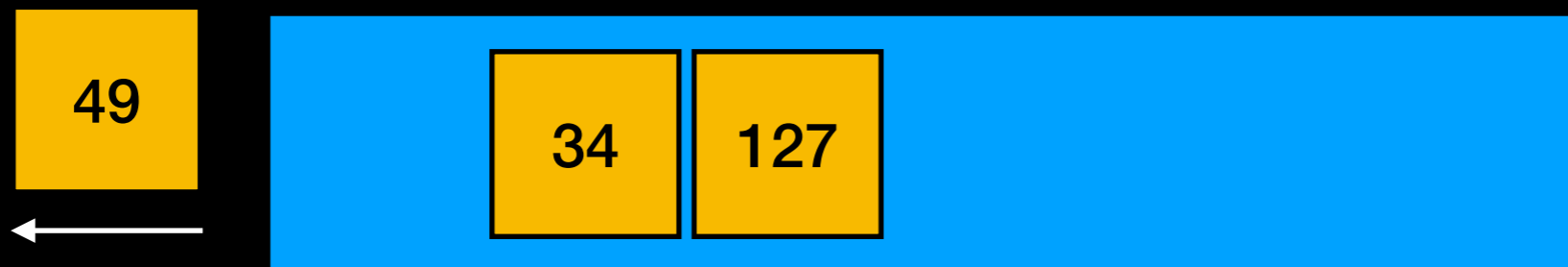
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In STL :

- does not use contiguous memory
- more complex to implement (keep track of memory blocks)
- grows more efficiently than vector

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- does not use contiguous memory
- more complex to implement (keep track of memory blocks)
- grows more efficiently than vector

In STL stack and queue are *adapters* of deque

STL standardized the use of "push" and "pop", adapting with "push_back", "push_front" etc. for all containers

Priority Queue

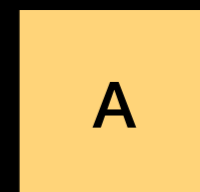
Low Priority



High Priority



A queue of items "sorted" by priority



Priority Queue

Low Priority



High Priority



A queue of items "sorted" by priority



Priority Queue

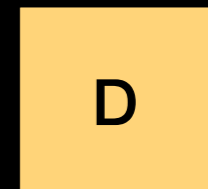
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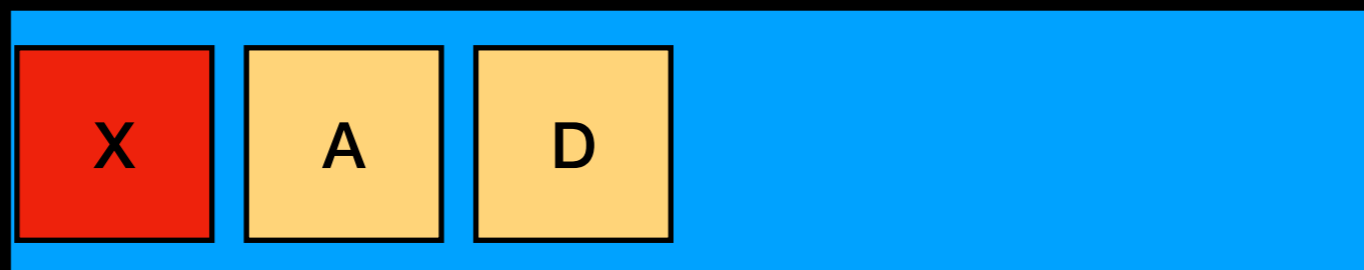
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Priority Queue

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Priority Queue

Low Priority



High Priority



A queue of items "sorted" by priority

If value indicates priority, it amounts to a sorted list that accesses/removes the "highest" items first



Priority Queue

Orders elements by priority => removing an element will return the element with highest priority value

Elements with same priority kept in queue order (in some implementations)

Priority Queue

Spoiler Alert!!!!

Often implemented with a **Heap**

Will tell you what it is in soon... but it is another example of ADT vs data structure